# IEEE Standard Practices and Requirements for Semiconductor Power Rectifier Transformers 

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#### Abstract

Practices and requirements for semiconductor power rectifier transformers for dedicated loads rated single-phase 300 kW and above and three-phase 500 kW and above are included. Static precipitators, high-voltage converters for dc power transmission, and other nonlinear loads are excluded. Service conditions, both usual and unusual, are specified, or other standards are referenced as appropriate. Routine tests are specified. An informative annex provides several examples of load loss calculations for transformers when subjected to nonsinusoidal currents, based on calculations provided in the standard. Keywords: eddy current losses, harmonic load losses, single-phase transformers, three-phase transformers, three-winding transformers, transformer load losses, two-winding transformers


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## Introduction

(This introduction is not part of IEEE Std C57.18.10-1998, IEEE Standard Practices and Requirements for Semiconductor Power Rectifier Transformers.)

Early editions of ANSI C57.18 were written for transformers used with pool cathode mercury arc rectifiers. The last revision date for ANSI C57.18 was 1964. That standard did not reflect the practices that have developed with the use of semiconductor rectifying or converting devices, nor did it reflect the latest transformer technology. As a result, much of it is inconsistent with current practices and with other related standards, such as ANSI C34.2*, that deal with semiconductor converters. This new standard is the result of the decision to write a new rectifier transformer standard instead of revising the old standard. Suggestions for improvement of these practices will be welcomed.

Basic impulse level (BIL) ratings for windings connected to converters are not specified by this standard. There are many practical reasons why windings connected to converters need not have a BIL test or rating. These windings are often high-current, low-voltage windings that will not produce ANSI standard waveforms when tested. Interleaved windings cannot be impulse tested easily. Usually the converter and the transformer are close coupled in a throat connection and not subject to lightning strikes. The converter usually cannot withstand normal transformer BIL ratings for the winding voltages to which they are connected. These conditions aren't always true, however. If a user wishes to have a BIL rating or test, this may be arranged through commercial negotiations and technical specifications that may override this standard. This should also be acknowledged by the transformer manufacturer during the bidding process.

Hottest-spot winding temperatures are referred to in this standard. These are not tested values. Hottest-spot temperatures cannot be measured from a practical standpoint on production units. Therefore, average winding temperatures plus a hottest-spot increment may be used. There is continuing work in other standards groups on this matter.

The methods of rating the transformer kVA and currents in previous editions of ANSI C57.18 were based on the rms equivalent of a rectangular current wave shape based on the dc rated load commutated with zero commutating angle. This is the rms kVA and current method. All of the tables in Clause 10 are based on this traditional method. A new approach is to base the transformer kVA and currents on the rms value of the fundamental current and kVA . This is the fundamental kVA and current method. The fundamental kVA method is in use in IEC standards. This approach needs to be reflected in ANSI C34.2 and ANSI C34.3 as well as in this standard. The traditional tables are retained in Clause 10 to maintain its method. Both kVA values will be shown on the nameplate to accommodate either method. Specifying engineers should clearly define whether they are specifying the traditional rms kVA or the fundamental kVA so as to avoid confusion. RMS kVA is beneficial to users who utilize their primary metering on the transformer to monitor load. The fundamental kVA is related directly to the real power used by the rectifier or convertor. The rms kVA can be determined when the fundamental kVA is given along with the harmonic spectrum for the load. The specifying engineer is always obligated to supply the harmonic spectrum in order to properly rate and design the transformer. The specifying engineer has overall system responsibility; definition of the harmonic spectrum is not the transformer manufacturer's responsibility. The difference between the two methods should result in only a small percentage error in kVA sizing, but in some cases it may be determined to be critical. Future coordination with ANSI C34.2 and ANSI C34.3 working groups should give a final direction with regard to kVA rating method.

Two cautionary notes are in order regarding testing.
First, errors may result when measuring losses on transformers with low power factors. Care must be exercised in making the loss measurements for rectifier transformers with high reactance and low losses. Test tol-

[^0]erances should be held to $3 \%$ throughout the ranges of reactance and losses so as to accurately measure stray losses for the harmonic calculations. There is ongoing work on this subject within the Loss Measurement Working Group of the Performance Characteristics Subcommittee.

Second, other errors regarding resistance readings for losses or temperature rise tests are possible on lowvoltage, high-current windings having very low resistance, often with bolted joints. Connection losses may alter normal resistance measurements. Work on this topic should be undertaken in the future.

The exact methodology for temperature rise testing using service losses enhanced with harmonics needs to be more fully developed. After this standard has been in use, it is expected that manufacturers and users will develop more detailed preferred methods. Experience will also provide insight as to whether there are any serious shortcomings in these methods. It is hoped that they will be found to be safely conservative. It is believed that some development time is necessary with the new approach before exact methods are prescribed.

Work should be done on future revisions to this standard to develop more detailed methods of interphase transformer loss testing. More precise methods for determining losses for commercial guarantee purposes, as well as thermal and magnetic capability, are needed. These were not attempted in this standard revision due to lack of time.

This standard was developed by a Working Group of the Subcommittee on Performance Characteristics of the IEEE Transformer Committee. The Working Group had the following membership:

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# IEEE Standard Practices and Requirements for Semiconductor Power Rectifier Transformers 

## 1. Overview

### 1.1 Scope

This standard includes semiconductor power rectifier transformers for dedicated loads rated

- Single-phase 300 kW and above
- Three-phase 500 kW and above

The scope of this standard excludes

- Static precipitators
- High-voltage converters for dc power transmission
- Other nonlinear loads


### 1.2 Mandatory requirements

When this standard is used on a mandatory basis, the words "shall" and "must" indicate mandatory requirements, and the words "should" and "may" refer to matters that are recommended and permitted, respectively, but not mandatory.

## 2. References

When the following standards and guides referred to in this standard are superseded by an approved revision, the latest revision shall apply.

ANSI C34.3-1973 (IEEE Std 444-1973), IEEE Standard Practices and Requirements for Thyristor Converters for Motor Drives. ${ }^{1}$

[^1]ANSI C57.12.10-1988, American National Standard for Transformers- 230 kV and Below 833/948 through 8333/10 417 kVA, Single-Phase, and 750/862 Through 60 000/80 000/100 000 kVA with Load Tap Chang-ing-Safety Requirements.

ANSI C57.12.51-1981, American National Standard Requirements for Ventilated Dry-Type Power Transformers 501 kVA and Larger, Three-Phase, with High-Voltage 601 to 34500 Volts, Low-Voltage 208Y/120 to 4160 Volts.

ANSI C57.12.70-1978 (Reaff 1993), American National Standard Terminal Markings and Connections for Distribution and Power Transformers.

IEEE Std 100-1996, IEEE Standard Dictionary of Electrical and Electronics Terms, Sixth Edition. ${ }^{2}$

IEEE Std 519-1992, IEEE Recommended Practices and Requirements for Harmonic Control in Electric Power Systems.

IEEE Std 995-1987, IEEE Recommended Practice for Efficiency Determination of Alternating-Current Adjustable-Speed Drives, Part 1—Load Commutated Inverter Synchronous Motor Drives. ${ }^{3}$

IEEE Std C57.12.00-1993, IEEE Standard General Requirements for Liquid-Immersed Distribution, Power, and Regulating Transformers.

IEEE Std C57.12.01-1989, IEEE Standard General Requirements for Dry-Type Distribution and Power Transformers Including Those with Solid Cast and/or Resin-Encapsulated Windings. ${ }^{4}$

IEEE Std C57.12.80-1978 (Reaff 1992), IEEE Standard Terminology for Power and Distribution Transformers.
IEEE Std C57.12.90-1993, IEEE Standard Test Code for Liquid-Immersed Distribution, Power, and Regulating Transformers and IEEE Guide for Short Circuit Testing of Distribution and Power Transformers.

IEEE Std C57.12.91-1995, IEEE Standard Test Code for Dry-Type Distribution and Power Transformers.
IEEE Std C57.91-1995, IEEE Guide for Loading Mineral-Oil-Immersed Transformers.

IEEE Std C57.96-1989, IEEE Guide for Loading Dry-Type Distribution and Power Transformers.

IEEE Std C57.110-1986 (Reaff 1992), IEEE Guide for Establishing Transformer Capability When Supplying Nonsinusoidal Load Currents.

## 3. Definitions

Terms used in this document, other than those described below, are defined in IEEE Std 100-1996 ${ }^{5}$. Some terms are restated here for emphasis because of the special application.

[^2]3.1 commutating impedance (rectifier transformer): The impedance that opposes the transfer of current between two secondary winding terminals of a commutating group, or a set of commutating groups.
3.2 percent impedance (rectifier transformer): The percent of rated primary winding voltage required to circulate current equivalent to rated kilovoltamperes in the primary winding with all secondary winding terminals short-circuited.

## 4. Symbols

$D_{\mathrm{x}} \quad$ Commutating reactance transformation constant (applies only to the first mode of operation after the light load transition)
$E_{\mathrm{d}} \quad$ Average dc voltage under load
$E_{\text {do }} \quad$ Theoretical dc voltage (average dc voltage at no load or light transition load assuming no overlap, no phase control, and zero forward voltage drop)
$E_{\mathrm{L}} \quad$ Alternating-current system line-to-line voltage (rms)
$E_{\mathrm{n}} \quad$ Alternating-current system line-to-neutral voltage (rms)
$E_{\mathrm{r}} \quad$ Direct voltage drop caused by resistance losses in transformer equipment
$E_{\mathrm{s}} \quad$ Transformer secondary winding line-to-neutral, open-circuit no-load voltage (rms)
$E_{\mathrm{x}} \quad$ Direct voltage drop caused by commutating reactance
$f \quad$ Frequency of ac power system
$F_{\text {HL-OSL }}$ Other stray loss harmonic loss factor
$F_{\text {HL-WE }}$ Winding eddy current harmonic loss factor
$h \quad$ Order of harmonic
$I_{\mathrm{h}} \quad$ Harmonic component of current of the order indicated by the subscript h
$I_{\mathrm{L}} \quad$ Alternating line current (rms)
$I_{\mathrm{p}} \quad$ Equivalent thermal test current on primary windings
$I_{\mathrm{pL}} \quad$ Alternating line current corresponding to the current in the primary winding during load loss test
$I_{\mathrm{S}} \quad$ Equivalent thermal test current on secondary windings
$I_{\mathrm{T}} \quad$ Equivalent thermal test current on tertiary windings
$I_{\mathrm{p}}^{\prime} \quad$ Rated current for the primary windings
$I^{\prime}$ s Rated current for the secondary windings
$I_{\mathrm{T}}^{\prime} \quad$ Rated current for tertiary windings
$P_{\mathrm{EC}} \quad$ Total winding eddy current and circulating current loss under test conditions
$P_{\text {EC-p }} \quad$ Primary winding eddy current and circulating current loss under test conditions
$P_{\text {EC-s }} \quad$ Secondary winding eddy current and circulating current loss under test conditions
$P_{E C-T} \quad$ Tertiary winding eddy current and circulating current loss under test conditions
$P_{\text {OSL }} \quad$ Total other stray loss under test conditions
$P_{\text {OSL-p }} \quad$ Primary winding other stray loss under test conditions
$P_{\text {OSL-s }} \quad$ Secondary winding other stray loss under test conditions
$P_{\text {OSL-T }}$ Tertiary winding other stray loss under test conditions
$P_{\mathrm{r}} \quad$ Transformer load losses in watts (including resistance and eddy current losses)
$P^{\prime}$ osL $\quad$ Total other stray loss expected at rectifier operation
$P^{\prime}$ osL-p Primary winding other stray loss expected at rectifier operation
$P^{\prime}$ oSL-s Secondary winding other stray loss expected at rectifier operation
$P^{\prime}$ osL-T Tertiary winding other stray loss expected at rectifier operation
$P^{\prime}$ EC Total eddy current and circulating current loss expected at rectifier operation
$P_{\text {EC-p }}^{\prime}$ Primary winding eddy current and circulating loss expected at rectifier operation
$P_{\text {EC-s }}^{\prime} \quad$ Secondary winding eddy current and circulating loss expected at rectifier operation
$P_{\text {EC-T }}^{\prime} \quad$ Tertiary winding eddy current and circulating loss expected at rectifier operation
PU Per unit of some defined base
$q \quad$ Pulse number of rectifier or number of rectifier phases
$R_{\mathrm{c}} \quad$ Line-to-neutral commutating resistance in ohms for a set of commutating groups
$R_{\mathrm{cn}} \quad$ Equivalent line-to-neutral commutating resistance in ohms for a set of commutating groups, referred to the primary winding of a rectifier transformer
$R_{\mathrm{p}} \quad$ Total ohmic resistance of primary windings at $\tau$
$R_{\mathrm{s}} \quad$ Total ohmic resistance of secondary windings at $\tau$
$R_{\mathrm{T}} \quad$ Total ohmic resistance of the tertiary winding at $\tau$
$t \quad$ Turns ratio (primary to secondary)
$\tau \quad$ Rated winding temperature rise plus $20^{\circ} \mathrm{C}$
$X_{\mathrm{c}} \quad$ Line-to-neutral commutating reactance in ohms for a set of commutating groups
$X_{\mathrm{cn}} \quad$ Equivalent line-to-neutral commutating reactance in ohms for a set of commutating groups referred to the primary winding of a rectifier transformer ( $X_{\mathrm{cn}}=D_{\mathrm{x}} X_{\mathrm{c}}$ )
$Z_{\mathrm{c}} \quad$ Line-to-neutral commutating impedance in ohms for a set of commutating groups
$Z_{\mathrm{cn}} \quad$ Equivalent line-to-neutral commutating impedance in ohms for a set of commutating groups referred to the primary winding of a rectifier transformer
$Z_{g} \quad$ Line-to-neutral commutating impedance in ohms for a single commutating group

## 5. Service conditions

### 5.1 Usual service conditions

### 5.1.1 General

Usual service conditions shall be as defined in IEEE Std C57.12.00-1993 for liquid-immersed rectifier transformers and in IEEE Std C57.12.01-1989 for dry-type rectifier transformers, except where clearly not applicable to rectifier transformers or where otherwise specified herein.

### 5.1.2 Operation above or below rated voltage or frequency

Rectifier transformers shall be capable of
a) Operating continuously above rated voltage or below rated frequency, at maximum rated kVA for any tap, without exceeding the limits of observable temperature rise in accordance with 6.12 when both the secondary voltage and volts per hertz do not exceed $105 \%$ of rated values and the operating frequency is at least $95 \%$ of rated value.
b) Operating continuously above rated voltage or below rated frequency, on any tap at no load, without exceeding limits of observable temperature rise in accordance with 6.12 when neither the voltage nor volts per hertz exceeds $110 \%$ of rated values.

### 5.1.3 Voltage harmonics

Rectifier transformers shall be capable of operating under load with voltage harmonics present, but within the limits established by IEEE Std 519-1992.

### 5.2 Unusual service conditions

### 5.2.1 General

Conditions other than those described in 5.1 are considered unusual service conditions and, when prevalent, should be brought to the attention of those who are responsible for the design and application of the transformer.

### 5.2.2 Loading at other than rated load

### 5.2.2.1 Liquid-immersed rectifier transformers

IEEE Std C57.12.00-1993 and IEEE Std C57.91-1995 define loading for other than rated load conditions for liquid-immersed rectifier transformers.

### 5.2.2.2 Dry-type rectifier transformers

IEEE Std C57.12.01-1989 and IEEE Std C57.96-1989 define loading for other than rated load conditions for dry-type rectifier transformers.

### 5.2.3 Unusual temperature and altitude conditions

Rectifier transformers may be used at a higher or lower ambient temperature or at higher altitudes than those specified in 5.1, but special consideration must be given to these applications. For unusual temperatures, the appropriate guides referenced in IEEE Std C57.12.00-1993 and IEEE Std C57.12.01-1989 apply. For altitude, Table 1, Table 2, and Table 3 in Clause 10 may serve as a guide.

### 5.2.4 Other unusual service conditions

Other unusual service conditions include the following:
a) Damaging fumes or vapors, excessive or abrasive dust, explosive dust or gases, steam, salt spray, excessive moisture or dripping water, etc.
b) Abnormal vibration, shocks, or tilting.
c) Unusual transportation or storage conditions.
d) Unusual space limitations.
e) Unusual operating duty, frequency of operation, difficulty of maintenance, poor wave form, unbalanced voltage, special insulation requirements, high source impedance, etc.
f) The presence of any dc current in transformer windings either from load or supply side.

### 5.2.5 Transformers energized from a convertor/inverter

Transformers energized from a convertor/inverter are often subject to considerably distorted voltages. Generally, voltage harmonics are considered to be low with regard to loss correction and negligible in thermal design considerations. If voltage distortions are known to be above the specified limits in IEEE Std 5191992, information shall be given in the specification with details of the service conditions.

Variable frequency applications are generally considered to be constant volts per hertz, unless noted otherwise. If the volts per hertz is variable, the degree of variation shall be given in the specification. The amplitude of the flux density in the core is the most important factor, not the maximum value of the nonsinusoidal voltage.

## 6. Rating data

The kVA rating of a rectifier transformer shall be the kVA drawn from the line.

### 6.1 Taps on rectifier transformers

If taps are provided they shall be considered to be, unless otherwise specified, only a means of adjusting for sustained departures in alternating supply voltage. These shall be rated kVA primary taps.

When taps are provided in the rectifier transformer for adjusting the output voltage, the taps providing output voltages above rated voltage shall be rated kVA taps, and the output current shall be reduced in proportion to the increase in output voltage, thereby maintaining rated kilowatt output. The taps providing output voltages below rated voltage shall be reduced kVA taps, the output currents shall not exceed the current specified, and voltage variation shall not exceed $\pm 10 \%$.

### 6.2 Cooling classes of transformers

Use "Cooling Classes of Transformers" in IEEE Std C57.12.00-1993 and "Limits of Temperature Rise" in IEEE Std C57.12.01-1989.

### 6.3 Frequency

The frequency of rectifier transformers covered by this standard shall be 60 Hz unless otherwise specified.

### 6.4 Phases

See Table 9 for selection of number of primary and secondary phases.

### 6.5 Rated kVA

### 6.5.1 Line kVA rating

The line kVA rating of a rectifier transformer shall be the kVA assigned to it by the specifier corresponding to the kVA drawn from the ac system at rated ac voltage and rated dc volts and dc amperes on the rectifier, not including auxiliary power.

### 6.5.2 RMS kVA rating

The traditional rms kVA ratings are shown in the tables and figures in Clause 10. These values are based on the rms equivalent of a rectangular current wave shape based on the dc rated load commutated with zero commutating angle. The rms kVA can also be calculated by calculating the rms value of the sum of the fundamental line current plus all of the associated harmonic line currents. The equivalent thermal test current will be used for testing thermal capability.

### 6.5.3 Fundamental kVA rating

The fundamental kVA rating is based on the rms value of the fundamental current and the fundamental line-to-line voltage. The fundamental kVA rating and line current shall be used for commercial loss guarantees.

### 6.6 Compensation on rectifier transformers

The specifier shall take the following aspects into account while arriving at the specification. In order to obtain rated direct output voltage at rated current on the rectifier unit, the winding turns ratio of the rectifier transformer may be changed to compensate for either or both of the following:
a) Momentary reduction in alternating supply voltage or prolonged operation at reduced alternating voltage without a tap change.
b) Voltage drop resulting from ac system impedance. When compensation is required, the following shall be specified:

1) Minimum alternating supply voltage at which the rectifier unit shall deliver rated direct voltage and current with the transformer on a specified voltage tap.
2) Maximum system impedance for which compensation is required. The impedance shall be given in ohms or in terms of short-circuit kVA or amperes available at the terminals of the primary winding of the rectifier transformer. The total number, capacities, and transformer connections of all rectifiers to be supplied by the same ac system shall also be specified.

NOTE-A rectifier transformer that is compensated by decreasing the winding turns ratio has an increased kVA rating.

It is the responsibility of the specifying engineer to provide the transformer manufacturer with the proper compensations. The specifying engineer must provide the values of $E_{\mathrm{s}}$, transformer kVA, and transformer impedance.

### 6.7 Rated current

### 6.7.1 RMS rated current method

The rated current of a rectifier transformer is the rms equivalent of a rectangular current wave shape based on the dc rated load commutated with zero commutating angle.

### 6.7.2 Fundamental current method

The rated current of a rectifier transformer is the rms equivalent of the fundamental component of the line current.

### 6.8 Connections

Rectifier transformer connections may be selected from Table 9 of Clause 10 as required.

### 6.9 Polarity, angular displacement, and lead markings

### 6.9.1 Polarity of single-phase rectifier transformers

All single-phase rectifier transformers shall have subtractive polarity.

### 6.9.2 Angular displacement between voltages for polyphase transformers

Figures 1, 2, and 3 show angular displacements for circuits 46,45 , and 53 , respectively. These examples may be expanded to include all circuit configurations.

### 6.9.3 Connection and marking of terminals for rectifier transformers

Rectifier transformer terminal markings shall be as follows:
a) The terminals of the primary windings of rectifier transformer equipment shall be marked " H " with subscripts.
b) The terminals of the secondary windings of rectifier transformer equipment shall be marked "R" with subscripts. If there is more than one group of secondary windings in the same phase position, successive groups shall be marked "S," "T," "U," "V," and "W" and auxiliary windings shall be "A." The corresponding phases shall have the same numerical subscripts. The neutral terminals of secondary windings shall be marked " N " with subscripts.

### 6.10 Impedance

### 6.10.1 Percent impedance of a rectifier transformer

See 3.2.

### 6.10.2 Commutating impedance

See 3.1 and 8.8.1.

This value is defined as one-half the total impedance in the commutating circuit expressed in ohms referred to the total secondary winding. For wye, star, and multiple wye circuits, this is the same value as derived in ohms on a phase-to-neutral voltage basis; while with diametric and zig-zag circuits it must be expressed as one-half the total due to both halves being mutually coupled on the same core leg or phase.

### 6.11 Losses

Use losses described in IEEE Std C57.12.00-1993 for liquid-immersed rectifier transformers and in IEEE Std C57.12.01-1989 for dry-type rectifier transformers.

### 6.12 Temperature rise and insulation system capability

"Temperature Rise and Insulation System Capability" in IEEE Std C57.12.01-1989 and "Temperature Rise and Loading Conditions" in IEEE Std C57.12.00-1993 shall be used for this standard.

## CAUTION

The application of some types of hottest-spot temperature measuring equipment to a rectifier transformer is complicated by the effect of residual dc magnetomotive forces due to various abnormal operating conditions of the rectifier. When hottest-spot temperature measuring equipment is provided, it is subject to inherent error due to abnormal operating conditions.

### 6.13 Nameplates

A nameplate shall be attached to each rectifier transformer. It shall be made of corrosion-resistant material with permanent easily visible engraved or stamped lettering.

### 6.13.1 Nameplate information

The minimum information shown on the nameplate shall be as specified below:
a) Serial number.

NOTE-The height of letters and numerals showing the serial number shall be a minimum of $4.0 \mathrm{~mm}(5 / 32 \mathrm{in})$. The height of other letters and numerals shall be at the manufacturer's discretion.
b) Cooling class. In some cases, it may be desirable to include the type or form, or both, in addition to the cooling class.
c) Number of primary winding phases.
d) Frequency.
e) kVA (line rating). Both the rms kVA rating and the fundamental kVA rating will be shown.

1) The height of letters and numerals showing kVA shall be 4.0 mm ( $5 / 32 \mathrm{in}$ ). The height of other letters and numerals shall be at the manufacturer's discretion.
2) Where the cooling class of a transformer involves more than one kVA rating, such as forced cooled class or future forced-cooling class, the kVA rating should be the line kVA corresponding to rated kW of rectifier. Supplemental rectifier transformer ratings, if specified, should be indicated by a note on the nameplate.
f) Voltage ratings.
3) The height of letters and numerals showing voltage ratings shall be a minimum of 4.0 mm (5/32 in), whether engraved or stamped. The height of other letters and numerals shall be at the manufacturer's discretion.
4) The primary winding voltage rating shall be the primary line voltage and circuit connection, and the secondary winding voltage rating shall be the voltage anode to neutral or line-to-line with reference to the circuit employed. Example: 13800 Y-745 anode to neutral, double Y.
g) Tap voltages.
5) The tap voltage of a winding shall be designated by listing the winding voltage of each tap separated by a slant, or it shall be in tabular form. The rated voltage of each tap shall be shown in volts.
6) The rated rms currents of all windings at rms kVA corresponding to the rated dc amperes of the rectifier shall be shown.
h) Temperature rise, ${ }^{\circ} \mathrm{C}$.
i) Polarity (single phase) or phasor diagram (polyphase).
j) Percent impedance at line kVA rating.
k) Commutating reactance in ohms, phase-to-neutral referred to total dc winding.
7) The following statement: "For use with a $\qquad$ phase ${ }^{6}$, $\qquad$ kW , $\qquad$ volts, dc, single, or double way, rectifier for $\qquad$ service" (electrochemical, industrial, light traction, mining, or heavy traction, extra heavy traction) Circuit \# $\qquad$
m) Approximate weights. The approximate weights in pounds (or kilograms) shall be shown as follows:

Core and coils $\qquad$
Tank and fittings $\qquad$
Liquid $\qquad$
Total weight $\qquad$
Untanking weight (heaviest piece) $\qquad$
n) Connection diagram.

[^3]All leads brought outside the tank and all windings shall be identified on the nameplate or connection diagram. (Show connections as viewed facing the transformer from the side on which the nameplate is attached or as otherwise described.)

A schematic view shall be included to show the relative location of external and internal terminals. In general, the schematic view should be arranged to show the secondary winding at the bottom and the H1 primary winding terminal at the top left. (The arrangement may be modified in particular cases, such as multiwinding transformers equipped with terminal chambers, potheads, or having terminal locations not conforming to the suggested arrangement if the modification is explained.)

All internal leads and terminals that are not permanently connected shall be designed or marked with numbers or letters in a manner which will permit convenient reference and will obviate confusion with terminal and polarity markings.
o) Patent numbers (at the manufacturer's discretion).
p) Name of manufacturer.
q) Reference to instruction book or sheet.
r) The words "rectifier transformer" and "dry-type" or "liquid-immersed."
s) Type of liquid if liquid-immersed or class of insulation if dry-type.
t) Number of gallons of liquid. The number of gallons of insulating liquid shall be shown for the main tank and for each liquid-immersed compartment.
u) Basic impulse level (BIL). BIL rating in kV of line terminals of windings shall be designated as the following example:

Primary winding ......................... 110 kV BIL
Secondary winding ....................... 45 kV BIL
v) Conductor material.
w) Date of manufacture.

### 6.13.2 Additional information

In addition to the information specified in 6.13.1, the following shall be included on the nameplate, when applicable:
a) Indication of provision for future forced-cooling equipment.
b) Indication of potential transformers, potential devices, current transformers, winding temperature devices, etc.
c) Polarity and location identification of current transformers to be shown if used for metering, relaying, or line-drop compensation. (Polarity need not be shown if current transformers are used for winding temperature equipment or fan control.)
d) Maximum operating pressures of liquid preservation system, kPa (or $\mathrm{lbf} / \mathrm{in}^{2}$ ) positive and
$\qquad$ $\mathrm{kPa}\left(\right.$ or $\mathrm{lbf} / \mathrm{in}^{2}$ ) negative.
e) Tank designed for $\qquad$ cm (inches) mercury vacuum.
f) Liquid level below top surface of the highest point of the highest manhole flange at $25^{\circ} \mathrm{C}$,
$\qquad$ cm (inches). Liquid level changes $\qquad$ cm (inches) per $10^{\circ} \mathrm{C}$ in liquid
temperature.
g) Core and coils braced for $\qquad$ times normal load current.

## 7. Construction

Use IEEE Std C57.12.00-1993 for construction specifications for liquid-immersed rectifier transformers, and IEEE Std C57.12.01-1989 for dry-type rectifier transformers in this standard except as follows.

### 7.1 Mounting and location

### 7.1.1 Portable mining-type rectifier transformer

A portable mining-type rectifier transformer shall be suitable for transporting on skids or wheels in the restrictive areas of mines.

### 7.1.2 Lifting, jacking, and/or skidding

Rectifier transformers shall be supplied with lifting, jacking, and/or skidding attachments. Special requirements for handling must be specified.

### 7.2 Tanks

### 7.2.1 Finish

The finish normally furnished by a manufacturer shall be supplied except as required by this subclause or as specified. Metallic flake paints, such as aluminum and zinc, etc., have properties which increase the temperature rise of the transformers except in direct sunlight. Temperature limits and tests are based upon the use of a pigment paint finish.

### 7.2.2 Bracing

Transformers shall be braced sufficiently to withstand normal forces experienced in shipping, maintaining, and operating.

### 7.3 Method of coolant preservation

Refer to ANSI C57.12.10-1988 for approved methods of coolant preservation.

### 7.4 Grounding

Grounding of case and core on liquid-immersed rectifier transformers shall be done as described in IEEE Std C57.12.00-1993. For dry-type rectifier transformers, grounding of case and core shall be done as described in IEEE Std C57.12.01-1989.

### 7.5 Connections for shipping

Unless otherwise specified, connection specifications in IEEE Std C57.12.00-1993 for liquid-immersed and IEEE Std C57.12.01-1989 for dry-type rectifier transformers shall apply.

### 7.6 Accessories

Accessories may include any or all of the following:

### 7.6.1 Liquid-immersed transformers

Liquid level gauge with alarm contact; cooling medium temperature gauge with one- or two-point alarm contacts; sudden pressure relay; gas-fault relay; pressure relief device with alarm; liquid flow switch with alarm; pressure-vacuum gauge with high and low alarm and bleeder; nozzles with valves for filling, draining, sampling, and liquid filtering; pump; manholes; weather-protected covers for controls and wiring terminal compartments; heat exchangers; radiators; and other. These shall be specified as required.

### 7.6.2 Dry-type transformers

Temperature detection device; fan and fan control circuit; space heater; ground protection relays; etc. These shall be specified by users.

## 8. Testing and calculations

Unless otherwise specified, tests shall be made at the factory only.

### 8.1 Routine tests

The following routine tests shall be made on all rectifier transformers. The numbers shown do not necessarily indicate the sequence in which the tests shall be made. All tests shall be made in accordance with the test code in IEEE Std C57.12.90-1993 for liquid-immersed transformers and the test code in IEEE Std C57.12.91-1995 for dry-type transformers.
a) Resistance measurements of all windings on the rated voltage connection of each identical unit and in case of a production run, at the tap extremes of one unit of a given rating when produced by one manufacturer at the same time.
b) Ratio tests on the rated voltage connection and on all tap connections.
c) Polarity and phase relation tests on the rated voltage connection.
d) Excitation loss at rated voltage on the rated voltage connection.
e) Excitation current at rated voltage on the rated voltage connection.
f) Impedance and load loss at rated current on the rated voltage connections of each unit (except as modified by 8.6) and on the tap extremes of one unit of a given rating when produced by one manufacturer at the same time.
g) Temperature test or tests shall be made on one unit when one or more units of a given rating are produced by one manufacturer at the same time, except that these tests shall be omitted when a record of a temperature test, made in accordance with these standards, on a duplicate or essentially duplicate unit, is available. The temperature test is a design test, not a routine test.

Subject to the limitation of the preceding paragraph, when a rectifier transformer is supplied with auxiliary cooling equipment to provide more than one kVA rating, temperature tests shall be made in accordance with Table 14 of IEEE Std C57.12.00-1993.
h) Applied potential tests.
i) Induced potential tests.

### 8.2 Symbols used in tests

Symbols listed in Clause 4 as used in routine tests may be modified by additional subscripts to indicate phase, line, transformer, etc. (i.e., $X_{\mathrm{c}}, X_{\mathrm{c} 2}, X_{\mathrm{c} 3}, X_{\mathrm{cl}}, X_{\mathrm{ct}}$ ). Additional symbols will be identified as used.

### 8.3 Resistance measurement

Use resistance measurement as described in IEEE Std C57.12.90-1993 for liquid-immersed and in IEEE Std C57.12.91-1995 for dry-type rectifier transformers as part of this standard.

### 8.4 Dielectric tests

Unless otherwise specified, dielectric tests shall be made in accordance with IEEE Std C57.12.90-1993 for liquid-immersed rectifier transformers and IEEE Std C57.12.91-1995 for dry-type rectifier transformers. Dielectric tests on rectifier transformer secondaries will be made using voltages given in Tables 4 and 5 in Clause 10 of this standard.

### 8.5 Excitation losses

Use excitation loss measurement as described in IEEE Std C57.12.90-1993 for liquid-immersed, and IEEE Std C57.12.91-1995 for dry-type transformers as part of this standard.

### 8.6 Load losses

Load losses of rectifier transformers shall be determined by the methods given in IEEE Std C57.12.90-1993 for liquid-immersed and in IEEE Std C57.12.91-1995 for dry-type units, with special considerations listed below. The measurement of load losses shall be performed with sinusoidal rated transformer current. The load loss guarantee is based on the sinusoidal loss measurement, for commercial purposes.

Actual service load losses for the expected harmonic spectrum provided in the specification supplied to the transformer manufacturer with the inquiry may also be calculated and submitted for information in the bid proposals. These losses are not subject to guarantee, but shall be calculated according to accepted methods, an example of which is described in the remainder of 8.6 , or by the use of an advanced mathematical modeling technique.

### 8.6.1 General

The difference in kVA capabilities of the primary and secondary windings of many rectifier transformers makes it impractical to circulate rated current in all windings when making load loss tests. Furthermore, the load loss is dependent on the magnitude and wave form of the current flowing in the windings. The current wave form is influenced by the circuit employed, by transformer reactance, and by the supply lines. Involved calculations are necessary to accurately include the effects of all these factors. Investigations have demonstrated, however, that tests made with sine wave currents having the same rms values as the expected rectangular current waves, together with calculations based thereon, permit load losses, accurate to within satisfactory limits, to be obtained. When making load loss tests on rectifier transformers, external interphase transformers, if present, shall be excluded from the test circuits in any manner that precludes their contributing to the losses measured. Internal interphase transformers shall be tested in accordance with 8.6.4.

### 8.6.2 Test and calculations required for load loss tests

a) Measure all winding resistances on a per winding basis and correct to $\tau$.
b) Use rated sinusoidal current (or multiples thereof as specified below) at rated frequency, and with indicated secondary windings shorted, test for load loss and correct to $\tau$ as described in IEEE Std C57.12.90-1993 for liquid-immersed and in IEEE Std C57.12.91-1995 for dry-type transformers.

The above methods will provide losses for the sinusoidal loss data for commercial guarantee purposes. To calculate approximate service losses, perform the remaining calculations c) through k ). These losses will be used for thermal tests. See Annex A for examples of these calculations. It is recognized that the loss method referenced will yield conservative results. More sophisticated mathematical methods may be used at the manufacturer's discretion.
c) Calculate $I_{\mathrm{p}}^{2} R_{\mathrm{p}}+I_{\mathrm{s}}^{2} R_{\mathrm{s}}$ in the tested windings using resistances from a) above, the currents from b) above, with the factors indicated below.
d) Subtract calculated loss in c) from tested loss in b) to obtain total stray loss.
e) Separate winding eddy current loss $\left(P_{\mathrm{EC}}\right)$ from other stray loss $\left(P_{\mathrm{OSL}}\right)$. (This is a function of the manufacturer's transformer design, rating, etc.)
f) If no data is available, a division of $60 \% P_{\mathrm{EC}}$ and $40 \% P_{\mathrm{OSL}}$ shall be specified.
g) If no data is available, the division of eddy current loss and other stray loss between windings is assumed to be as follows:

1) Sixty percent in the low-voltage winding and $40 \%$ in the high-voltage winding for all transformers having a maximum self-cooled current rating of less than 1000 A (regardless of turns ratio).
2) Sixty percent in the low-voltage winding and $40 \%$ in the high-voltage winding for all transformers having a turns ratio of $4: 1$ or less.
3) Seventy percent in the low-voltage winding and $30 \%$ in the high-voltage winding for all transformers having a turns ratio greater than $4: 1$ and also having one or more windings with a maximum self-cooled current rating greater than 1000 A .
h) The harmonic composition of the load for full-load rectifier operation shall be specified to the transformer manufacturer. The transformer manufacturer does not have the necessary system information needed to predict the harmonic characteristics of the load. Transformers manufactured to this standard do not generate the harmonics to which they are subjected. Equipment manufactured to rectifier and converter standards generate the harmonics in conjunction with the system to which they are applied. Developments within these standards groups affect the harmonics produced by the rectifier or converter equipment. Rectifier and converter equipment of the same pulse order, but of differing applications or even differing manufacturers, may produce different harmonic spectrums. Each application and location can provide its own unique characteristics. IEEE Std 519-1992 should be used for guidance. The specifying engineer must assume the responsibility of supplying the harmonic spectrum to the transformer manufacturer. In the event that a user cannot supply an appropriate harmonic spectrum, the transformer manufacturer may refer to Table 11 of Clause 10 for an appropriate spectrum, which is generally conservative.

## CAUTION

This spectrum may not be appropriate for the actual application. It should submitted in the transformer manufacturer's quotation to the specifying engineer and accepted only when no better information is available.
i) Winding eddy current losses are known to increase by the square of the current applied as well as the square of the frequency applied. It is possible to calculate, to give a close approximation, the additional losses due to distorted load currents by multiplying the winding eddy current losses at fundamental frequency by a single numerical value, rather than calculate each individual frequency. $F_{\mathrm{HL}-}$ wE is the per unit multiplier of the winding eddy current losses. This factor is normalized to either
the fundamental or the rms current (square root of the sum of the harmonic currents squared). In either case, $F_{\mathrm{HL}-\mathrm{WE}}$ remains the same value, since it is a function of the harmonic current distribution and is independent of the relative magnitude. The factor may be calculated using actual measured or calculated currents or may be determined from normalized per unit values of load current. In terms of the perunit load current, the winding eddy current harmonic loss factor is defined as
$F_{\mathrm{HL}-\mathrm{WE}}=\frac{\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2} h^{2}}{\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2}}$
If the square root of the sum of the harmonic currents squared equals the rms sine wave current under rated frequency and load conditions, and if the per unit current base is the rated current, this equation may also be written in a more simple form as
$F_{\mathrm{HL}-\mathrm{WE}}=\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2} h^{2}$

Escalate eddy current loss in all windings by

$$
\begin{equation*}
P_{\mathrm{EC}}^{\prime}=P_{\mathrm{EC}-\mathrm{p}}\left(F_{\mathrm{HL}-\mathrm{WE}}\right)+P_{\mathrm{EC}-\mathrm{s}}\left(F_{\mathrm{HL}-\mathrm{WE}}\right) \tag{3}
\end{equation*}
$$

j) In the treatment of harmonic losses used in IEEE Std C57.110-1986 (Reaff 1992) ${ }^{7}$ and other documents, a conservative approach is often used. In these standards, other stray losses are escalated by the same factors as winding eddy current losses. It is known that stray losses increase with the square of the magnitude of the load current. Studies have shown, however, that the eddy current losses in bus bars and connections increase only by a harmonic exponent factor of 0.8 or less, instead of a squared factor. Other studies by manufacturers and others have shown that stray losses in structural parts also increase by a harmonic exponent factor of 0.8 or less. Therefore, the value of the harmonic exponent of 0.8 shall be used in other stray loss harmonic loss calculations in this document.

Similar to the treatment in i) above, the other stray loss harmonic loss factor will be defined as $F_{\text {HL-OSL }}$. This is the per unit multiplier of the other stray losses measured in test at fundamental frequency. In terms of the per unit load current, the other stray loss harmonic loss factor is defined as
$F_{\mathrm{HL}-\mathrm{OSL}}=\frac{\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2} h^{0.8}}{\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2}}$
If the square root of the sum of the harmonic currents squared equals the rms sine wave current under rated frequency and load conditions, and if the per unit current base is the rated current, this equation may also be written in a more simple form as

$$
\begin{equation*}
F_{\mathrm{HL}-\mathrm{OSL}}=\sum_{1}^{n} I_{\mathrm{h}}(\mathrm{pu})^{2} h^{0.8} \tag{5}
\end{equation*}
$$

[^4]Escalate other stray loss by

$$
\begin{equation*}
P_{\mathrm{OSL}}^{\prime}=P_{\mathrm{OSL}-\mathrm{p}}\left(F_{\mathrm{HL}-\mathrm{OSL}}\right)+P_{\mathrm{OSL}-\mathrm{s}}\left(F_{\mathrm{HL}-\mathrm{OSL}}\right) \tag{6}
\end{equation*}
$$

k) Total loss for each shorted winding configuration corresponding to full-load rectifier operation $\left(P_{\mathrm{A}}\right.$, $P_{\mathrm{B}}, P_{\mathrm{C}}$ ) is equal to

$$
\begin{equation*}
I_{\mathrm{p}}^{\prime}{ }^{2} R_{\mathrm{p}}+I_{\mathrm{s}}^{\prime}{ }^{2} R_{\mathrm{s}}+P_{\mathrm{EC}}^{\prime}+P_{\mathrm{OSL}}^{\prime} \tag{7}
\end{equation*}
$$

It is recognized that the above treatment of harmonic losses may not be completely accurate due to the actual site conditions; the actual harmonic spectrum (which may vary over time); the actual loss distributions within the windings of the transformer; the inability to conduct these tests at the actual harmonic frequencies; the approximations and assumptions made; etc. However, these calculations should give reasonably correct values of losses for the determination of transformer capability under harmonic conditions. Actual transformer losses under rectifier load conditions may be somewhat higher or lower than the above calculations. Also, there may still be a hottest-spot problem on a transformer under actual load conditions, which may not be detected if tested with losses as calculated above due to loss distributions. Nevertheless, this treatment of losses will provide greater recognition of the harmonic losses present in rectifier transformers under actual operating conditions than has been previously afforded when the losses have only been treated as sinusoidal losses.

### 8.6.3 Loss tests for special rectifier transformer connections

The following tests shall be performed to calculate the losses on special rectifier transformer connections. Performing the loss tests as given below will provide sinusoidal load-loss data for the purpose of commercial guarantee. The power input to the primary windings under these conditions, corrected as described in 8.6.2, will give, within satisfactory limits, the approximate service load losses that correspond to operation of the rectifier at rated load. These service load losses shall be used for thermal tests.
a) For rectifier transformer connections as shown in circuit numbers 2, 8, 9, 41, 43, 45, 46, 47, 48, 49, 52 , and 66 , measure the load loss as follows:

Short circuit one-half of the secondary windings associated with each phase of the primary windings and hold sinusoidal rated current at rated frequency in the primary windings. This test shall be repeated, but with the other half of the secondary windings shorted, and the average of the two corrected power readings taken as the load loss.

For circuit no. 9 , the test current used during the test shall be 1.224 times the rated primary line current, determined from the transformer rated kVA (as given on the nameplate), because the kVA rating of the primary is equal to 1.224 times the rated primary line kVA. Similarly for circuit no. 43 , the sinusoidal line current used during the test shall be 1.06 times the rated ac line current. Also, for circuit no. 52 , the sinusoidal line current during the test shall be 1.035 times the rated ac line current.
b) For circuit numbers 53 and 54 when the primary windings consists of a single circuit associated with all of the secondary windings, two load loss tests are necessary.

1) Short circuit the secondary windings groups used with any two of the simple rectifier circuits and hold sinusoidal rated current at rated frequency in the primary windings. Measure the power input to the primary windings and designate as $P_{\mathrm{A}}$.
2) Short circuit all of the secondary windings and hold sinusoidal rated current at rated frequency in the primary windings. Measure the power input to the primary windings and designate as $\mathrm{P}_{\mathrm{B}}$.

The transformer load losses, $P_{\mathrm{r}}$, will be calculated by the following equation:

$$
\begin{equation*}
P_{\mathrm{r}}=1.14 P_{\mathrm{A}}-0.14 P_{\mathrm{B}} \tag{8}
\end{equation*}
$$

For circuit numbers 53A and 54A when the primary windings consist of two paralleled circuits, each of which is associated with only two of the groups of secondary windings, the load loss test is as follows:

Short circuit one of the secondary winding groups associated with each of the two primary winding circuits and hold 1.035 times sinusoidal rated current at rated frequency in the primary windings. This test shall be repeated, but with the other secondary winding groups shorted, and the average of the two corrected power readings taken as the load loss.
c) For circuit numbers 11,12 , and 56, three load loss tests are required as follows:

Hold sinusoidal rated current at rated frequency in the primary winding terminals for each of the secondary winding short circuits listed in Table 7. Measure the power input to the primary winding in each case, and designate as $P_{\mathrm{A}}, P_{\mathrm{B}}$, and $P_{\mathrm{C}}$, respectively.

The transformer load losses, $P_{\mathrm{r}}$, calculated within satisfactory limits by the following equation:
$P_{\mathrm{r}}=\frac{P_{\mathrm{A}}+2 P_{\mathrm{B}}+3 P_{\mathrm{C}}}{6}$

For circuit no. 56, the sinusoidal line current used during the test shall be 1.035 times rated primary line current.
d) For double-way circuit numbers 21 to 28 , inclusive, $30,33,34,35 \mathrm{~A}$, and 68 , which have the same voltampere rating for both primary and secondary windings, the load losses are determined by short circuiting all the secondary windings and passing sinusoidal rated current at rated frequency through the primary windings. The power input to the primary windings will give the load losses directly.
e) For circuit no. 31 when the primary windings consist of a single circuit associated with all the secondary windings, three load loss tests are required:

1) Short circuit all of the secondary windings and hold sinusoidal rated current at rated frequency in the primary windings. Measure the power input to the primary windings and designate as $P_{\mathrm{A}}$.
2) Repeat test 1) with one set of secondary windings shorted and designate these measured losses as $P_{\mathrm{B}}$.
3) Repeat test 1) with the other set of secondary windings shorted and designate these measured losses as $P_{\mathrm{C}}$.

The transformer load losses, $P_{\mathrm{r}}$, will be calculated within satisfactory limits by the following equation:

$$
\begin{equation*}
P_{\mathrm{r}}=0.932 P_{\mathrm{A}}+0.034\left(P_{\mathrm{B}}+P_{\mathrm{C}}\right) \tag{10}
\end{equation*}
$$

For circuit no. 31 when the primary winding consists of two paralleled circuits, each associated with one secondary winding group, test as in d) except that the sinusoidal line current during test shall be 1.035 times rated primary line current.
f) For any transformer connections as considered above but having two or more identical in phase groups of secondary windings operated in parallel or in series, such as circuit numbers $32,42,50$, $50 \mathrm{~A}, 51,51 \mathrm{~A}, 61,62,63$, and 64 , like numbered terminals of the several groups shall be connected together for the purpose of making load loss tests. The groups thus connected shall, for the purpose of this test, be considered as one group.
g) For circuit no. 29, if the primary winding consists of a single circuit associated with all of the secondary windings, the load losses are determined by short circuiting one group of secondary windings and passing sinusoidal rated current at rated frequency through the primary windings. The power input to the primary windings will give, within satisfactory limits, the transformer load loss.

This test shall be repeated with the other group of secondary windings shorted and the average of the two power readings shall be designated the load loss.

For circuit no. 29, if the primary windings consist of two parallel circuits, each of which is associated with one group of secondary windings, the load loss is determined by the method described in d) above. A sinusoidal line current equal to $\sqrt{2}$ times the rated primary line current shall be used during the test.
h) For circuit numbers $1,3,4,5,6,7,13,14,65$, and 67 , sinusoidal rated current, $I_{\mathrm{p}}$, shall be passed through the primary windings during test with all secondary windings shorted. This test gives $P_{\text {A. }}$. Then,
$P_{\mathrm{r}}=P_{\mathrm{A}}+I_{\mathrm{s}}{ }^{2} R_{s}\left[1-\left(t I_{\mathrm{p}}^{\prime} / I_{\mathrm{s}}\right)^{2}\right]$
i) For circuit no. 10, a sinusoidal current equal to $1.224 I_{\mathrm{p}}$ shall be passed through the primary windings during test with all secondary windings shorted; the increase over the rated current is required to provide for the ampere turns of the tertiary windings, which carry no current during this test. The turn ratio $t$ is equal to the ratio of the phase-to-neutral voltage of the primary windings to twice the phase-to-neutral voltage of the secondary windings. This test gives $P_{\mathrm{A}}$. Then,

$$
\begin{equation*}
P_{\mathrm{r}}=P_{\mathrm{A}}-0.5\left(I_{\mathrm{p}}^{\prime}\right)^{2} R_{\mathrm{p}}+\left(I_{\mathrm{s}}^{\prime}\right)^{2} R_{\mathrm{s}}\left[1-1.5\left(t I_{\mathrm{p}}^{\prime} / I_{\mathrm{s}}^{\prime}\right)^{2}\right]+\left(I_{\mathrm{T}}^{\prime}\right)^{2} R_{\mathrm{T}} \tag{12}
\end{equation*}
$$

j) For circuit no. 44, a sinusoidal current equal to $1.06 I_{\mathrm{p}}$ shall be passed through the primary winding during test with all secondary windings shorted. The turn ratio $t$ is equal to the ratio of the phase-toneutral voltage of the primary windings to twice the phase-to-neutral voltage of the secondary windings. This test gives $P_{\mathrm{A}}$. Then,

$$
\begin{equation*}
P_{\mathrm{r}}=P_{\mathrm{A}}-0.125\left(I_{\mathrm{p}}^{\prime}\right)^{2} R_{\mathrm{p}}+\left(I_{\mathrm{s}}^{\prime}\right)^{2} R_{\mathrm{s}}\left[1-1.125\left(t I_{\mathrm{p}}^{\prime} / I_{\mathrm{s}}^{\prime}\right)^{2}\right]+\left(I_{\mathrm{T}}^{\prime}\right)^{2} R_{\mathrm{T}} \tag{13}
\end{equation*}
$$

Circuit numbers 15 and 55 consist of two sets of windings, having independent magnetic circuits. One set has primary windings connected in delta, and is similar to circuit no. 9 . The other set has primary windings connected to wye and a delta connected tertiary winding and is similar to circuit no. 10. The load losses for the set with the delta connected primary windings are determined in the same way as for circuit no. 9 above. The load losses for the set with the wye connected primary windings are determined as prescribed for circuit no. 10 above. The total load losses are equal to the sum of the load losses for the two sets of windings.
k) For combined circuit numbers 25 and 26, a sinusoidal current of 0.518 times rated total $I_{\mathrm{p}}$ shall be passed through the primary windings with the secondary windings corresponding to the delta primary shorted. This test shall be $P_{\mathrm{A}}$. Repeat this test with the secondary windings corresponding to the wye primary shorted. This test shall be $P_{\mathrm{B}}$. Total loss corresponding to full-load rectifier operation is

$$
\begin{equation*}
P_{\mathrm{r}}=P_{\mathrm{A}}+P_{\mathrm{B}} \tag{14}
\end{equation*}
$$

### 8.6.4 Load losses in interphase transformers, anode paralleling reactors, and commutating reactors

The interphase transformer load losses shall be ohmic losses computed from the resistance of the windings corrected to and the current corresponding to operation of the rectifier at rated load.

When either or both of these reactors are mounted as an integral part of the rectifier transformer, their load losses shall be measured simultaneously with, and included as part of, the rectifier transformer load losses.

Terminals that connect to rectifying elements which operate in parallel shall be connected together during the load loss tests.

When this equipment is mounted remotely from the rectifier transformer, the load losses shall be measured by circulating sinusoidal rated current at rated frequency between the transformer terminals and the corresponding rectifier terminals connected together. The power input during this test shall be the load loss.

### 8.7 Losses in interphase transformers

### 8.7.1 Excitation losses

The excitation losses of interphase transformers shall be measured with an applied sine wave voltage having the same average value and the same fundamental frequency as the voltage appearing on the same terminals when the rectifier is operating at rated load.

If facilities are not available for tests at this frequency, the test may be made at any frequency within $15 \%$ of the desired value by applying a voltage corrected in proportion to the desired frequency. The losses shall then be taken as the measured loss multiplied by the ratio of desired frequency to test frequency.

An alternate method is to measure the losses at two or more frequencies by applying voltage corrected in proportion to those frequencies and determine the losses at the desired frequency by interpolation.

### 8.7.2 Load losses

The interphase transformer load losses shall be as described in 8.6.4.

### 8.8 Impedance tests

### 8.8.1 Transformer impedance

Short circuit all secondary winding terminals and apply voltage to primary winding terminals at rated frequency and adjust to circulate current equivalent to the rated line kVA in the primary windings.

### 8.8.2 Determination of transformer commutating reactance

Two methods are available. Method No. 1 is general and applicable to all circuit connections. Method No. 2 for rectifier transformers whose secondary windings have high current ratings and low reactance. Limited testing facilities may dictate that the test be made by shorting two secondary winding terminals between which commutation occurs and applying single phase sinusoidal primary voltage at rated frequency on appropriate primary winding terminals. Method No. 2 is applicable only when the secondary windings of the rectifier transformer are not interconnected between phases. Method No. 1 requires a specific test. Method No. 2, where applicable, uses the results of the load loss test when made according to 8.6.

### 8.8.2.1 Direct Method No. 1

Short circuit all terminals of the primary winding of the rectifier transformer. Hold sinusoidal current at rated frequency on two secondary winding terminals between which commutation occurs. Take readings of the applied volts, amperes, and watts.

For any transformer connection having two or more identical in-phase groups of secondary windings operated in parallel or in series, such as circuit numbers $32,42,50,50 \mathrm{~A}, 51,51 \mathrm{~A}, 61,62,63$, and 64 , like-numbered terminals of the several groups shall be connected together for the purpose of making the tests.

One-half of the voltage measured during this test, divided by the current held, is the line-to-neutral commutating impedance, $Z_{\mathrm{c}}$, in ohms. This test should be repeated for each appropriate pair of secondary winding terminals in turn and the average of the results taken as the commutating impedance. One half of the watts, $P_{\mathrm{r}}$, measured on this test, divided by the square of the current held, is the line-to-neutral commutating resistance, $R_{\mathrm{c}}$, in ohms.

The line-to-neutral commutating reactance, $X_{\mathrm{c}}$, is determined as follows:

$$
\begin{equation*}
X_{\mathrm{c}}=\sqrt{\left(Z_{\mathrm{c}}\right)^{2}-\left(R_{\mathrm{c}}\right)^{2}} \tag{15}
\end{equation*}
$$

When anode paralleling reactors or commutating reactors are employed, they may be included in the circuit for this test or their reactance and resistance in ohms, as determined from the load loss test, may be added to the corresponding transformer values.

### 8.8.2.2 Indirect Method No. 2

For circuit numbers $9,21,23,24,25,32,33,35,35 \mathrm{~A}, 45,46,49,50,50 \mathrm{~A}, 51,51 \mathrm{~A}, 52,62$, and 68 , and other similar circuits in which neither the primary nor secondary windings have interconnections between phases, the commutating reactance can be calculated from the line-to-neutral voltage, $E_{\mathrm{z}}$, line current, $I_{\mathrm{pL}}$, and watts, $P_{\mathrm{r}}$, measured during the load loss test described in 8.6 as follows:

$$
\begin{align*}
& Z_{\mathrm{cn}}=\frac{E_{\mathrm{z}}}{I_{\mathrm{pL}}}  \tag{16}\\
& R_{\mathrm{cn}}=\frac{P_{\mathrm{r}}}{3\left(I_{\mathrm{pL}}\right)^{2}}  \tag{17}\\
& X_{\mathrm{cn}}=\sqrt{\left(Z_{\mathrm{cn}}\right)^{2}-\left(R_{\mathrm{cn}}\right)^{2}}  \tag{18}\\
& X_{\mathrm{c}}=X_{\mathrm{cn}}\left(\frac{\left(E_{\mathrm{s}}\right)^{2}}{\left(E_{\mathrm{n}}\right)^{2}} \times \frac{1}{D_{\mathrm{x}}}\right) \tag{19}
\end{align*}
$$

NOTE—See Table 8 for the values of $D_{\mathrm{x}}$.

### 8.9 Ratio tests

Use IEEE Std C57.12.90-1993 and IEEE Std C57.12.91-1995 for ratio tests on rectifier transformers, as applicable.

### 8.10 Temperature rise test

The temperature rise on rectifier transformers is determined by methods described in IEEE Std C57.12.901993 for liquid-immersed transformers, and in IEEE Std C57.12.91-1995 for dry-type transformers, except the winding losses used shall be the calculated service losses enhanced with harmonic losses.

### 8.10.1 Dry-type transformers

The test procedure shall be as described in IEEE Std C57.12.91-1995, with the exceptions noted in the following subclauses.

### 8.10.1.1 Core loss

The excitation loss portion of the temperature rise test remains as it is in IEEE Std C57.12.91-1995.

### 8.10.1.2 Load loss

The load loss test is modified to simulate service load losses. Service load losses shall be the tested load losses at the fundamental enhanced by the harmonics as calculated in 8.6. Test currents shall be increased to produce the service load losses for full-load rectifier operation, as calculated in 8.6. It is acknowledged that this will probably cause disproportionate heating in the individual windings during this test since the losses cannot be applied directly to the windings where they are produced, simultaneously. Typically, higher service loss windings will test lower in temperature rise than they should, while lower service loss windings will test higher in temperature rise than they should. The thermal test current used should be limited, if necessary, so as not to damage any windings or components that might be overloaded during the test. Correct the tested winding temperature rises by the correction methods for watts loss and current, as necessary, based on the appropriate cooling class and temperature rise test method used, as provided in IEEE Std C57.12.91-1995 for dry-type transformers.

Exceptions: If the rectifier and transformer are connected for this test, with an appropriate load connected to the rectifier (not a short-circuit type test), use rated currents.

### 8.10.2 Liquid-immersed transformers

Either of two load loss temperature rise methods of testing may be used. The procedure shall be the same as described in IEEE Std C57.12.90-1993, "Short-Circuit Method," except that the total losses shall include service load losses, excitation losses, and interphase transformer losses (if applicable). The service load losses shall be tested load losses at the fundamental enhanced by the harmonics as calculated in 8.6.

### 8.10.2.1 Load Loss Method A

The load loss test is modified to simulate service load losses. Service load losses shall be the tested load losses at the fundamental enhanced by the harmonics as calculated in 8.6. Test currents shall be increased to produce the service load losses for full-load rectifier operation, as calculated in 8.6. It is acknowledged that this will probably cause disproportionate heating in the individual windings during this test since the losses cannot be applied directly to the windings where they are produced, simultaneously. Typically, higher service loss windings will test lower in temperature rise than they should, while lower service loss windings will test higher in temperature rise than they should. The thermal test current used should be limited, if necessary, so as not to damage any windings or components that might be overloaded during the test. Correct the tested winding temperature rises by the correction methods for watts loss and current, as necessary, based on the appropriate cooling class and temperature rise test method used, as provided in IEEE Std C57.12.90-1993 for liquid-immersed transformers. This method may be performed in one test sequence.

### 8.10.2.2 Load Loss Method B

This method should generally follow the procedure described under 11.5.2.1, "Short-Circuit Method," in IEEE Std C57.12.90-1993.

The total loss supplied, in order to determine liquid rises, should include all losses specified in 8.10 .2 of this standard.

For the portion of the test as descried in IEEE Std C57.12.90-1993, where "rated current" is held for a duration of 1 h , this current will be modified to the equivalent thermal test current causing the equivalent calculated losses, enhanced with harmonics, to be present in the winding. This current may be calculated as follows:

$$
\begin{aligned}
& I_{\mathrm{p}}=I_{\mathrm{p}}^{\prime} \times C_{\mathrm{p}} \\
& I_{\mathrm{s}}=I_{\mathrm{s}}^{\prime} \times C_{\mathrm{s}}
\end{aligned}
$$

where

$$
\begin{align*}
& C_{\mathrm{p}}=\sqrt{\left[\left(I_{\mathrm{p}}^{\prime}\right)^{2} \times R_{\mathrm{p}}+P_{\mathrm{EC}-\mathrm{p}} \times F_{\mathrm{HL}-\mathrm{WE}}\right] /\left[I_{\mathrm{p}}^{\prime} \times R_{\mathrm{p}}+P_{\mathrm{EC}-\mathrm{p}}\right]}  \tag{20}\\
& C_{\mathrm{s}}=\sqrt{\left[\left(I_{\mathrm{s}}^{\prime}\right)^{2} \times R_{\mathrm{s}}+P_{\mathrm{EC}-\mathrm{s}} \times F_{\mathrm{HL}-\mathrm{WE}}\right] /\left[\left(I_{\mathrm{s}}^{\prime}\right)^{2} \times R_{\mathrm{s}}+P_{E C-s}\right]} \tag{21}
\end{align*}
$$

A separate 1 h test is required for each winding group (individually followed by shutdown and resistance measurements). However, no correction factor for loading should be required as in Load Loss Method A.

The thermal test current should be limited, if necessary, so as not to damage any windings or components that may be overloaded during test. If test currents are limited, correct the tested winding temperature rises by the correction methods for watts loss and current as necessary, based on the appropriate cooling class and temperature rise test method used, as provided in IEEE Std C57.12.90-1993 for liquid-immersed transformers.

Exceptions: If rectifier and transformer are connected for this test, with an appropriate load connected to the rectifier (not a short-circuit type test), use rated currents.

### 8.10.3 Other

The temperature rise test of a transformer containing dc windings that are connected to a single-way rectifier shall be tested with the rectifier in place and the primary current held to 1.1 of its rating. Compromises must be made if a rectifier is not available for a combinational test. A short-circuit heat run may be made in two steps. The first step is with all dc windings shorted and the rated current held on the primary windings. The result of this test shall be used to report the primary winding temperature rise. A second heat run shall be made holding primary current as high as possible without damaging the coil. This current may be calculated from the first heat run. The temperature rise of the dc windings must now be corrected for actual current to be held using the correction factor of IEEE Std C57.12.90-1993 for liquid-immersed units and IEEE Std C57.12.91-1995 for dry-type units. A compromise of testing one dc winding at a time is possible with reasonable results if the dc windings are not connected thermally. The dc winding temperature rise test may be made by short circuiting one of the dc windings and applying rated rms current to the other dc winding. This test can only be made if a suitable high-current source is available.

### 8.11 Short-circuit tests

When specified, short-circuit tests on rectifier transformers shall be conducted as described in IEEE Std C57.12.90-1993 for liquid-immersed transformers and in IEEE Std C57.12.91-1995 for dry-type transformers.

### 8.12 Polarity and phase relation

Use IEEE Std C57.12.90-1993 and IEEE Std C57.12.91-1995 for polarity and phase rotation tests on both liquid-immersed and dry-type rectifier transformers.

### 8.12.1 Polarity

Polarity tests are to made on single-phase transformers only. Follow the methods specified in IEEE Std C57.12.90-1993 for liquid-immersed transformers or IEEE Std C57.12.91-1995 for dry-type transformers.

### 8.12.2 Phase relation

### 8.12.2.1 Phase relation tests

Phase relation tests are made to determine angular displacement and relative phase sequence.

### 8.12.2.2 Test for phasor diagram

The phasor diagram of any three-phase rectifier transformer, defining both angular displacement and phase sequence, can be verified by connecting the H1 and R1 leads together, exciting the unit at a suitably low, three-phase voltage, taking voltage measurements between various pairs of leads, and then either plotting these values or comparing them for their relative order of magnitude with the help of the corresponding diagram in Figures 1, 2, and 3.

### 8.12.2.3 Phasor diagrams

Figures 4 through 7 give typical voltage phasor diagrams of circuits used in rectifier transformers.

### 8.12.2.4 Limitations

This method is practically limited to transformers in which the ratio of transformation is 30 to 1 or less, otherwise the difference between readings will be minimal.

### 8.12.2.5 Separate neutrals

When the neutral lead of each commutating group is brought out separately, the neutral leads have to be connected together for the test for phasor diagram.

## 9. Tolerances

### 9.1 Tolerances for ratio

Tolerances shall be as described in IEEE Std C57.12.00-1993 for liquid-immersed rectifier transformers, and in IEEE Std C57.12.01-1989 for dry-type rectifier transformers.

### 9.2 Tolerances for impedance

Tolerances for impedance of rectifier transformers shall be as described in IEEE Std C57.12.00-1993 for liq-uid-immersed transformers and in IEEE Std C57.12.01-1989 for dry-type transformers.

### 9.3 Tolerances for losses

Tolerances for losses of rectifier transformers shall be as described in IEEE Std C57.12.00-1993 for liquidimmersed transformers and in IEEE Std C57.12.01-1989 for dry-type transformers.

## 10. Figures and tables

This clause contains all the figures and tables referenced in Clauses 5, 6, and 8.

### 10.1 Figures

| ANGULAR DISPLACEMENT |   |
| :---: | :---: |
| DIAGRAM FOR CHECK <br> MEASUREMENTS |  |
| CHECK <br> MEASUREMENTS | CONNECT H1 TO R1 <br> MEASURE H3-R3,H3-R5,H1-H3,H2-R3,H2-R5,R1-R3,R1-R5 <br> VOLTAGE RELATIONS: <br> (1) R1-R3 = R1-R5 <br> (2) $\mathrm{H} 2-\mathrm{R} 3=\mathrm{H} 3-\mathrm{R} 5$ <br> (3) $\mathrm{H} 3-\mathrm{R} 3=\mathrm{H} 2-\mathrm{R} 5$ <br> (4) $\mathrm{H} 2-\mathrm{R} 3<\mathrm{H} 2-\mathrm{R} 5$ <br> MEASURE R1-R2,R2-R3,R3-R4,R4-R5,R5-R6,R6-R1 <br> VOLTAGE RELATIONS: ALL VOLTAGES ARE EQUAL |

Figure 1-Typical voltage phasor diagrams, circuit no. 46

| ANGULAR DISPLACEMENT |  |
| :---: | :---: |
| $\begin{aligned} & \text { DIAGRAM FOR } \\ & \text { CHECK } \\ & \text { MEASUREMENTS } \end{aligned}$ |  |
| CHECK <br> MEASUREMENTS | CONNECT H1 TO R1 <br> MEASURE H3-R3,H3-R5,H1-H3,H2-R3,H2-R5,R1-R3,R1-R5 <br> VOLTAGE RELATIONS: <br> (1) H3-R3 $=\mathrm{H} 3-\mathrm{R} 5$ <br> (2) $\mathrm{H} 3-\mathrm{R} 3<\mathrm{H} 1-\mathrm{H} 3$ <br> (3) H2-R3 < H2-R5 <br> (4) $\mathrm{H} 2-\mathrm{R} 3<\mathrm{H} 1-\mathrm{H} 3$ <br> MEASURE R1-R2,R2-R3,R3-R4,R4-R5,R5-R6,R6-R1 <br> Voltage relations: all voltages are equal |

Figure 2-Typical voltage phasor diagrams, circuit no. 45

| ANGULAR DISPLACEMENT |  |
| :---: | :---: |
| $\begin{aligned} & \text { DIAGRAM FOR } \\ & \text { CHECK } \\ & \text { MEASUREMENTS } \end{aligned}$ |  |
| CHECK <br> MEASUREMENTS | CONNECT H1 TO R1 <br> MEASURE R1-R5,R1-R9,H2-R5,H2-R9,H3-R5,H3-R9 <br> VOLTAGE RELATIONS: <br> (1) $\mathrm{H} 2-\mathrm{R} 5=\mathrm{H} 3-\mathrm{R} 9$ <br> (2) R1-R5 < R1-R9 <br> (3) H3-R9 < H3-H5 <br> (4) $\mathrm{H} 2-\mathrm{R} 5<\mathrm{H} 2-\mathrm{H} 9$ <br> MEASURE R1-R2,R2-R3,R3-R4,R4-R5,R5-R6,R6-R7,R7-R8 R8-R9,R9-R10,R10-R11,R11-R12,R12-R1 <br> VOLTAGE RELATIONS: ALL VOLTAGES ARE EQUAL |

Figure 3-Typical voltage phasor diagrams, circuit no. 53
1.

2.

3.

4.

5.

delta, three phase, zig-zag (WTE)
6.


WTE, THREE PHASE, ZIG-ZAG (WTE)



SCOTT, THREE PHASE, SCOTT (WTE)
8.



SCOTT, FOUR PHASE, CROSS
9.

detta, six phase, star
10.

11.


12.

13.

14. $\overbrace{\mathrm{H}_{3}}^{\mathrm{H}_{2}}$

15.


Figure 4—Rectifier circuits (simple, single-way circuits)
21.


DUMEIRIC, DOUBLE - WAY (BRIDGE)
22.



SCOIT, FOUR PHASE, OPEN + CROSS, DOUBLE-WAY
23.

DELTA, SIX PHASE, WEE, DOUBE-WAY
24.


WTE, SIX PHASE, WYE
DOUBLE-WAY




Wre, SIX PHASE,
DELTA, DOUBLE-WAY
27.


DELTA, SIX PHASE, ZIG-ZAG, DOUBLE-WAY
28.


WFE, SIX PHASE, ZIG-ZAG, DOUBLE-WAY
29.


DELTA, TWEIVE PHASE,
30.

31.

delta, twelve phase, multiple DELTA-WYE, DOUBLE-WAY

31A.

32.


32A.



Figure 5-Rectifier circuits (double-way circuits)



DEETA, SIX PHASE, DOUBLE WYE DOUBLE-WAY, THREE WRE WTH SINGLE INTERPHASE TRANSFORMERS

Figure 6—Rectifier circuits (double-way circuits) (Continued)

41


SCOTT, FOUR PHASE, DOUBLE
42


SCOTT, FOUR PHASE, PARALLE DOVBLE DCAMEIRIC

43

deLTA six PHASE, TRIPLE DWMETRIC


WTE. WTH TERTARY, SIX PHASE, TRIPLE DAMETRIC
45

deETA, SIX PHASE, DOUBLE WTE
46


WHE, SIX PHASE, DOUBLE WTE
47


delta, six phase, double zig-zag, (whe)


48



WTE, SIX PHASE, DOUBLE ZIG-ZAG, (WTE)


WTE, SIX PHASE, DOUBLE WTE WTHOUT INIERPHASE * * THREE SINGEE - PHASE CORES OR MAGNETIC EQUNALENT

50

delta, six phase, parnulel double wte WTH SINGLE INTERPHASE TRANSFORMER

50A



DELTA, SIX PHASE, PARALLEL DOUBLE WTE WTH TWO INTERPHASE TRANSFORMERS

51



WTE, SIX PHASE, PARALIEL DOUBLE WTE WTH SINGLE INIERPHASE TRANSFORMER


WTE, SIX PHASE, PARALIEL DOUBLE WTE WTH TWO INTERPHASE TRANSFORMERS

Figure 7—Rectifier circuits (multiple circuits, single-way)


WTE DELTA, TWEVE PHASE, QUNDRUPLE WHE

detid twelve phase, quadruple zig-zig wr


DETA, TWELVE PHASE, QUADRUPLE ZIG-ZAG (WTE) WTH TWO A.C. WNDINGS


WHE, TWELVE PHASE, QUADRUPLE ZIG-ZAG (WHE)


WTE DELTA, WTH TERTARY, TWELVE PHASE, DOUBLE STAR

delta whe, twelve phase, double fork (Star)

57

delta twelve phase, dovele zig-zag (Star)
Figure 8—Rectifier circuits (multiple circuits, single-way) (Continued)



HALF WAVE, SHUNTNG TUBE
66


DAWETRIC, SHUNTING TUBE

67


DEITA, THREE PHASE WE, SHUNTING TUBE
68



DELTA, SIX PHASE, SPUT FORK (STAR)
Figure 9—Rectifier circuits (miscellaneous circuits)

### 10.2 Tables

Table 1—Maximum allowable average temperature ( ${ }^{\circ} \mathrm{C}$ ) of cooling air for carrying rated kVA at altitudes of $1000 \mathrm{~m}(3300 \mathrm{ft})$ and greater

| Method of cooling apparatus | $\begin{gathered} 1000 \mathrm{~m} \\ (\mathbf{3 3 0 0} \mathrm{ft}) \end{gathered}$ | $\underset{(6600 \mathrm{ft})}{2000 \mathrm{~m}}$ | $\underset{(9900 \mathrm{ft})}{3000 \mathrm{~m}}$ | $\begin{gathered} 4000 \mathrm{~m} \\ (13200 \mathrm{ft}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
| Liquid-immersed self-cooled | 30 | 28 | 25 | 23 |
| Liquid-immersed forced-air-cooled | 30 | 26 | 23 | 20 |
| Liquid-immersed forced-liquid-cooled with liquid-to-air cooler | 30 | 26 | 23 | 20 |
| Dry-type Class AA |  |  |  |  |
| $80^{\circ} \mathrm{C}$ rise | 30 | 26 | 22 | 18 |
| $150{ }^{\circ} \mathrm{C}$ rise | 30 | 22 | 15 | 7 |
| Dry-type AA/FA and AFA |  |  |  |  |
| $80^{\circ} \mathrm{C}$ rise | 30 | 22 | 14 | 6 |
| $115{ }^{\circ} \mathrm{C}$ rise | 30 | 18 | 7 | -5 |
| $150{ }^{\circ} \mathrm{C}$ rise | 30 | 15 | 0 | -15 |

NOTE—Data for dry-type transformers only applies to ventilated type.

Table 2-Rated kVA derating factors for altitudes greater than $1000 \mathrm{~m}(3300 \mathrm{ft})$

| Types of cooling | Derating factor <br> $(\%)$ |
| :--- | :---: |
| Dry-type, self-cooled | 0.3 |
| Dry-type, forced-air-cooled | 0.5 |
| Liquid-immersed air-cooled | 0.4 |
| Liquid-immersed water-cooled | 0.0 |
| Liquid-immersed forced-air-cooled | 0.5 |
| Liquid-immersed forced-liquid-cooled <br> with liquid-to-air cooler | 0.5 |
| Liquid-immersed forced-liquid-cooled <br> with liquid-to-water cooler | 0.0 |

${ }^{\text {a }}$ The derating percentages are for each $100 \mathrm{~m}(330 \mathrm{ft})$ above 1000 m (3300 ft).

Table 3-Dielectric strength correction factors for altitudes greater than $1000 \mathbf{m}$ ( $\mathbf{3 3 0 0} \mathbf{f t}$ )

| Altitude <br> $(\mathbf{m})$ | Altitude <br> (ft) | Altitude correction <br> factor for dielectric <br> strength |
| :---: | :---: | :---: |
| 1000 | 3300 | 1.00 |
| 1200 | 4000 | 0.98 |
| 1500 | 5000 | 0.95 |
| 1800 | 6000 | 0.92 |
| 2100 | 7000 | 0.89 |
| 2400 | 8000 | 0.86 |
| 2700 | 9000 | 0.83 |
| 3000 | 10000 | 0.80 |
| 3600 | 12000 | 0.75 |
| 4200 | 14000 | 0.70 |
| 4500 | 15000 | 0.67 |

NOTE—An altitude of $4500 \mathrm{~m}(15000 \mathrm{ft})$ is considered a maximum for transformers conforming to this standard.

Table 4—Dielectric tests for secondary windings ${ }^{\text {a }}$

| Maximum crest $\mathbf{b}$ <br> voltage to ground | Dielectric test levels for secondary windings, <br> low-frequency tests |  |
| :---: | :---: | :---: |
| $\mathbf{V}$ | Liquid-immersed <br> $\mathbf{k V}$, rms | Dry-type kV, <br> rms |
| $1200^{\text {c }}$ | $10^{\text {c }}$ | $5^{\text {c }}$ |
| 2500 | 15 | 10 |
| 5000 | 19 | 12 |
| 8600 | 26 | 19 |
| 15000 | 34 | 31 |

${ }^{\text {a }}$ See 8.4.
${ }^{\mathrm{b}}$ See Table 5.
${ }^{c}$ Interleaved windings present a special case. These are typically low voltage and do not have high dielectric stresses to one another. These windings must be subject to full hi-pot tests to ground. Unless specified otherwise, the hi-pot levels to one another will be twice the operating voltage plus 1000 V , rounded up to the nearest 500 V , but in no case less than 2500 V .

Table 5—Formulas for secondary windings maximum crest voltage to ground (see 8.4)

| Circuit number <br> (Table 13) | Peak inverse voltage | Ground point | Maximum crest voltage to ground |
| :---: | :---: | :---: | :---: |
| 1,65 | $\sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{aligned} & \sqrt{2} E s \\ & \sqrt{2} E s \end{aligned}$ |
| $\begin{aligned} & 2,8,9,10,11, \\ & 12,13,14,15,61 \\ & 62,63,64,66 \end{aligned}$ | $2 \sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{gathered} 2 \sqrt{2} E s \\ \sqrt{2} E s \end{gathered}$ |
| $3,4,5,6,7,67$ | $\sqrt{6} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{aligned} & \sqrt{6} E s \\ & \sqrt{2} E s \end{aligned}$ |
| 21, 22 | $2 \sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{aligned} & 2 \sqrt{2} E s \\ & 2 \sqrt{2} E s \end{aligned}$ |
| $\begin{aligned} & 23,24,25,26, \\ & 27,28,29,32 \end{aligned}$ | $\sqrt{6} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{aligned} & \sqrt{6} E s \\ & \sqrt{6} E s \end{aligned}$ |
| 30 | $2 \sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{array}{r} 2 \sqrt{2} E s \\ \sqrt{2} E s \end{array}$ |
| 31 | $\sqrt{6} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ | $\begin{aligned} & \sqrt{6} E s \\ & \sqrt{6} E s \end{aligned}$ |
| 33, 34 | $\sqrt{6} E s$ | $\begin{aligned} & + \text { bus } \\ & \text { - bus } \end{aligned}$ <br> neutral bus | $\begin{aligned} & \sqrt{6} E s \\ & \sqrt{6} E s \\ & \sqrt{2} E s \end{aligned}$ |
| 35, 35A | $2 \sqrt{2} E s^{\text {a }}$ | + bus <br> - bus <br> neutral bus | $\begin{gathered} 2 \sqrt{2} E s \\ 2 \sqrt{2} E s \\ \sqrt{2} E s \end{gathered}$ |
| 41, 42 | $2 \sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & - \text { bus } \end{aligned}$ | $\begin{array}{r} 2 \sqrt{2} E s \\ 1.5 \sqrt{2} E s \end{array}$ |
| 43, 44 | $2 \sqrt{2} E s$ | $\begin{aligned} & + \text { bus } \\ & - \text { bus } \end{aligned}$ | $\begin{array}{r} 2 \sqrt{2} E s \\ 1.66 \sqrt{2} E s \end{array}$ |

NOTE-All formulas for crest voltage to ground are based upon the ground-point location as shown in the table. Other ground point locations may exist in the application of the transformer for which the crest voltage may be expected to be higher than the tabulated formula. An example of such a system is an ac motor drive. If the motor side of the drive is grounded, then the crest voltage at the transformer secondary will be the result of the switching action of two converters, instead of only one rectifier. The transformer specifier must communicate any increased voltage to ground requirement in order to assure that the transformer will have suitable insulation levels.
${ }^{\text {a }}$ These values are the maximum that may exist and are used for dielectric test purposes only. For the peak inverse voltage during normal operation, the correct value is $\sqrt{6} E s$.

Table 5-Formulas for secondary windings maximum crest voltage to ground (see 8.4) (Continued)

| Circuit number (Table 13) | Peak inverse voltage | Ground point | Maximum crest voltage to ground |
| :---: | :---: | :---: | :---: |
| $45,46,47,48,49,50$, 50A, 51, 51A, 52, 53, 53A, 54 | $2 \sqrt{2} E s^{\text {a }}$ | $\begin{aligned} & + \text { bus } \\ & - \text { bus } \end{aligned}$ | $\begin{array}{r} 2 \sqrt{2} E s \\ \sqrt{2} E s \end{array}$ |
| 55, 56, 57 | $2 \sqrt{2} E s$ | $\begin{aligned} & \text { + bus } \\ & \text { - bus } \end{aligned}$ | $\begin{array}{r} 2 \sqrt{2} E s \\ 1.067 \sqrt{2} E s \end{array}$ |
| 68 | $4 \sqrt{2} E s$ | $\begin{gathered} \text { + bus } \\ \text { - bus } \\ \text { Capacitor midpoint } \end{gathered}$ | $\begin{aligned} & 4 \sqrt{2} E s \\ & 4 \sqrt{2} E s \\ & 2 \sqrt{2} E s \end{aligned}$ |

NOTE-All formulas for crest voltage to ground are based upon the ground-point location as shown in the table. Other ground point locations may exist in the application of the transformer for which the crest voltage may be expected to be higher than the tabulated formula. An example of such a system is an ac motor drive. If the motor side of the drive is grounded, then the crest voltage at the transformer secondary will be the result of the switching action of two converters, instead of only one rectifier. The transformer specifier must communicate any increased voltage to ground requirement in order to assure that the transformer will have suitable insulation levels.
${ }^{\text {a }}$ These values are the maximum that may exist and are used for dielectric test purposes only. For the peak inverse voltage during normal operation, the correct value is $\sqrt{6} E s$.

## Table 6-Electrical characteristics of liquid-insulated rectifier transformer equipment bushings

| Secondary winding maximum voltage crest to ground kV <br> (1) | Voltage class primary winding kV | BIL kV (2) | Outdoor bushings |  |  | Indoor bushings (4) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 60 Hz withstand |  | Impulse full-wave drywithstand $1.2 \times 50 \mu \mathrm{~s}$ kV | 60 Hz drywithstand 1 min kV | Impulse <br> full-wave drywithstand $1.2 \times 50 \mu \mathrm{~s}$ kV |
|  |  |  | $1 \min _{k V} \text { dry }$ | $\begin{aligned} & 10 \text { s wet } \\ & \text { kV (3) } \end{aligned}$ |  |  |  |
| 1.2 |  |  |  |  |  |  |  |
| 2.5 |  |  | 21 | 20 |  | 20 |  |
| 5.0 |  |  | 27 | 24 |  | 24 |  |
| 8.7 |  |  | 35 | 30 |  | 30 |  |
| 15.5 |  |  | 50 | 45 |  | 50 |  |
|  |  |  |  |  |  |  |  |
|  | 1.2 | 45 |  |  |  |  |  |
|  | 2.5 | 60 | 21 | 20 | 60 | 20 | 45 |
|  | 5.0 | 75 | 27 | 24 | 75 | 24 | 60 |
|  | 8.7 | 95 | 35 | 30 | 95 | 30 | 75 |
|  |  |  |  |  |  |  |  |
|  | 15.0 | 110 | 50 | 45 | 110 | 50 | 110 |
|  | 25.0 | 150 | 70 | 70 | 150 | 60 | 150 |
|  | 34.5 | 200 | 95 | 95 | 200 | 80 | 200 |
|  | 46.0 | 250 | 120 | 120 | 250 |  |  |
|  |  |  |  |  |  |  |  |
|  | 69.0 | 350 | 175 | 175 | 350 |  |  |
|  | 92.0 | 450 | 225 | 190 | 450 |  |  |
|  | 115.0 | 550 | 280 | 230 | 550 |  |  |

## NOTES

1-The insulation level of secondary windings is determined by maximum crest voltage to ground in kV .
2-The BIL of the primary winding bushings should not be less than the BIL of the primary winding.
Unless specified and agreed to in advance, impulse testing of secondary windings is not a requirement, due to the special nature of rectifier applications. Bifilar or interleaved windings shall not be tested to one another. Bifilar or interleaved windings may be impulse tested to ground or to the high-voltage winding, only if specified and agreed to in advance.
Typically, one cannot achieve standard impulse test waveforms due to the high capacitance of these windings. Per normal impulse test methods, it would be acceptable to tie all of the terminals together for the impulse test. Again, impulse testing of windings connected to converter terminals is not a requirement of this standard.
3-Wet withstand values are based on water resistivity of $427 \Omega / \mathrm{cm}^{3}\left(7000 \Omega / \mathrm{in}^{3}\right)$ and precipitation rate of $0.5 \mathrm{~cm} / \mathrm{min}$ ( $0.2 \mathrm{in} / \mathrm{min}$ ).
4-Indoor bushings are those intended for use on indoor transformers. Indoor bushing test values do not apply to bushings used primarily for mechanical protection of insulated cable leads. A wet test value is not assigned to indoor bushings.

Table 7-Terminals to be shorted on load-loss test circuit numbers 11, 12, and 56

| Circuit no. | Test A | Test B | Test C |
| :--- | :--- | :--- | :--- |
| 11 and 12 | R1-R2 | R2-R3 | R1-R3-R5 |
|  | R3-R4 | R4-R5 | or |
|  | R5-R6 | R6-R1 | R2-R4-R6 |
| 56 | R1-R3 | R3-R5 | R1-R5-R9 |
|  | R5-R7 | R7-R9 | R2-R6-R10 |
|  | R9-R11 | R11-R1 | or |
|  | R2-R4 | R4-R6 | R3-R7-R11 |
|  | R6-R8 | R8-R10 | R4-R8-R12 |
|  | R10-R12 | R12-R2 |  |

Table 8-Commutating reactance transformation constant for various rectifier circuits

| Circuit no. | Value of $\boldsymbol{D}_{\mathbf{x}}$ | Notes |
| :--- | :---: | :---: |
| 2,21 | 1 | $E n=E L / 2$ |
| $3,4,5,6$, <br> $23,24,25,26,27,28$, <br> $31,32,33,34,35,35 \mathrm{~A}$, <br> $45,46,47,48,49$, <br> $50,51,52,53,54,50 \mathrm{~A}$, <br> $66,67,51 \mathrm{~A}, 53 \mathrm{~A}, 54 \mathrm{~A}$ |  |  |
| 8,61 | 1 |  |
| $9,10,11,12,13,14$, <br> $55,56,57$, <br> $62,63,64$ |  |  |
| 15 | $3 / 2$ | Three-phase supply |
| 22 | 3 |  |
| 29 | $3 / 8$ |  |
| $30,41,42$ | $(2+\sqrt{3})$ |  |
| 43,44 | $3 / 4$ |  |

Table 9-Rectifier circuits and properties

| ANSI CIRCUIT NUMBER \& NAME |  | $2 \quad$DUMEIRIC <br> (FULL WAVE) | 5. DELTA, THREE PHASE <br> 5. ZIG-ZAG (WVE) | WFE, THREE PHASE 6. ZIG-ZAG (WYE) |
| :---: | :---: | :---: | :---: | :---: |
| NUMBER PHASES AC WINDING |  | 1 | 3 | 3 |
| NUMEER PHASES DC WDG. ( $\mathrm{n} \times \times \times \mathrm{p}=\mathrm{q}$ ) |  | 2 | 3 | 3 |
| PHASOR DMGRAM |  |  |  |  |
| ANODE CURRENT | WAVE FORM |  |  |  |
|  | AVERAGE | $I_{d} / 2$ | $I_{d} / 3$ | $I_{\text {d }} / 3$ |
|  | RMS | $I_{d} / \sqrt{2}$ | $\mathrm{I}_{\mathrm{d}} / \sqrt{3}$ | $I_{d} / \sqrt{3}$ |
| D.C. WNDING CURRENT | WAVE FORM | SAME AS anode current | SAME AS anode current | SAME AS anode current |
|  | FORM FACTOR |  |  |  |
|  | RMS | $I_{d} / \sqrt{2}$ | $I_{d} / \sqrt{3}$ | $\mathrm{I}_{\mathrm{d}} / \sqrt{3}$ |
|  | KVA RATING | $\sqrt{2} I_{d E} \times \times 10^{-3}$ | $2 I_{d} E \times 10^{-3}$ | $2 I_{d} E s \times 10^{-3}$ |
| A.C. WINDING CURRENT | WAVE FORM |  |  |  |
|  | FORM FACTOR | 1.00 | 1.23 | 1.23 |
|  | RMS | $I_{d \times E} / E_{L}$ | $\sqrt{2} / 3 \times I_{d} \times E_{s} / E_{L}$ | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{s} / E_{L}$ |
|  | KVA RATING | $I_{d} E_{8} \times 10^{-3}$ | $\sqrt{2} I_{d} E_{s} \times 10^{-3}$ | $\sqrt{2} I_{d} E_{8} \times 10^{-3}$ |
| A.C. LINE CURRENT | WAVE FORM | SAME AS <br> AC WINDING CURRENT |  | same as <br> AC WINDING CURRENT |
|  | FORM FACTOR | 1.00 | 1.08 | 1.23 |
|  | RMS | SAME AS AC WINDING | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{B} / E_{L}$ | SAME AS AC WINDING |
|  | KVA RATING | SAME AS AC WINDING | SAME AS AC WINDING | SAME AS AC WINDING |
| - C Voltage - Edo |  | 0.9 Es | 1.17 E : | $1.17 \mathrm{Es}_{8}$ |
| DC REACTIVE VOLTAGE DROP Ex |  | $0.31 \mathrm{Id}_{\mathrm{d}}$ | $0.477 \mathrm{I}_{\mathrm{d}} \times \mathrm{c}$ | $0.477 \mathrm{I}_{\mathrm{d}} \times \mathrm{c}$ |
|  |  | 1 | 1 | 1 |
| PEAK INVERSE VOLTAGE |  | $2 \sqrt{2} \mathrm{Es}$ | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
| $\begin{aligned} & \text { max cress } \\ & \text { youthe } 1 \\ & \text { cound (4) } \end{aligned}$ | + BUS GROUNDED | $2 \sqrt{2}$ E8 | $\sqrt{6} \mathrm{Es}$ | $\sqrt{6} \mathrm{Es}$ |
|  | - BUS GROUNDED | $\sqrt{2} \mathrm{Es}$ | $\sqrt{2} \mathrm{Es}$ | $\sqrt{2} \mathrm{Es}$ |
| TOTAL WINDING LOSSES FROM TESTS | TEST | R1 TO No | R1-R2-R3 | R1-R2-R3 |
|  | " $A$ " | RATED RMS CURRENT | RATED RMS CURRENT | RATED RMS CURRENT |
|  | TEST ${ }^{\text {che }}$ | R2 TO No |  |  |
|  | $\text { " } B^{n} \left\lvert\, \begin{array}{ll} 100 \\ 0 & 0 \\ 0 \end{array}\right.$ | RATED RMS CURRENT |  |  |
|  | TEST Wend |  |  |  |
|  |  |  |  |  |
|  |  | $\frac{P_{A}+P_{B}}{2}$ | $P_{A}+\frac{1}{9} I^{2}{ }_{d} R_{S}$ | $P_{A}+\frac{1}{9} I^{2}{ }_{d} R_{S}$ |
|  |  | METHOD NO. 1 | METHOD NO. 1 | METHOD NO. 1 |

Table 9—Rectifier circuits and properties (Continued)

| ANSI CIRCUIT N | UMBER \& MAME | 8. SCOTT, FOUR PHASE | 9. DELTA, STXX PHASE | 11. DELTA, SIX PHASE | WYE, SIX PHASE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MUMBER PHASES AC WNONVG |  | 3 | 3 | 3 | 3 |
| MUMEER PHASES DC WDG. ( $n \times s \times p=q$ ) |  | 4 | 6 | 6 | 6 |
| PHASOR DHGRAM |  |  |  |  |  |
| ANODE CURRENT | WAVE FORM |  |  |  |  |
|  | AVERAGE | $I_{\text {d } / 4}$ | $I_{\text {d }} / 6$ | $I_{d} / 6$ | $I_{d} / 6$ |
|  | RMS | $\mathrm{I}_{\mathrm{d}} / 2$ | $I_{d} / \sqrt{6}$ | $I_{d} / \sqrt{6}$ | $I_{d} / \sqrt{6}$ |
| D.C. WMDNNG CURRENT | WAVE FORM | SAWE AS ANODE CURRENT | SAME AS <br> ANODE CURRENT |  |  |
|  | FORM FACTOR |  |  |  |  |
|  | RWS | $I_{d / 2}$ | $1 / \sqrt{6} \quad I_{d}$ | " ${ }^{\prime \prime} \mathrm{COM}=I_{d} / \sqrt{6}$ | "b" COHL $=I_{d} / \sqrt{3}$ |
|  | KVA RATNG | $2 I_{d} E_{s} \times 10^{-3}$ | $\sqrt{6} I_{d E s} \times 10^{-3}$ | $(1+\sqrt{2}) E_{s} I_{d} \times 10^{-3}$ | $(1+\sqrt{2}) E_{8} I_{d} \times 10^{-3}$ |
| A.C. WMDNNG CURRENT | WAVE FORM |  |  |  |  |
|  | FORM FACTOR | 1.04/1.41 | 1.73 | 1.23 | 1.23 |
|  | RMS | $\sqrt{2} / \sqrt{3 \times} I_{d \times} \times E_{s} / E_{L}$ | $I_{d} / \sqrt{3} \times E_{s} / E_{L}$ | $\sqrt{2} / 3 \times I_{d} \times E_{8} / E_{L}$ | $\sqrt{2} / \sqrt{3 \times} I_{d} \times E_{s} / E_{L}$ |
|  | KVA Ratwig | $1.525 \mathrm{I}_{d} \mathrm{E}_{s} \times 10^{-3}$ | $\sqrt{3} I_{d} E s \times 10^{-3}$ | $\sqrt{2} I_{d} E_{s} \times 10^{-3}$ | $\sqrt{2} I_{d} E s \times 10^{-3}$ |
| A.C. LINE CURRENT | WAVE FORM | SAME AS <br> AC WMNDNG CURRENT |  |  | SAME AS <br> AC WMNDING CURRENT |
|  | FORM FACTOR | 1.04/1.41 | 1.23 | 1.06 | 1.23 |
|  | RMS | SAME AS AC WINDING | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{s} / E_{L}$ | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{s} / E_{L}$ | SAME AS AC WNDNG |
|  | KVA RATING | $\sqrt{2} I_{d}$ Es $\times 10^{-3}$ | $\sqrt{2} I_{d} E_{s} \times 10^{-3}$ | $\sqrt{2} I_{d} E s \times 10^{-3}$ | SAME AS AC WMNDNG |
| DC VOLTAGE - E do |  | 1.27 Es | 1.35 Es | 1.35 Es | 1.35 Es |
| DC REACTIVE VOLTAGE DROP E $\times$ |  | $0.637 \mathrm{I}_{\mathrm{d}} \mathrm{X} \mathrm{c}_{\text {c }}$ | $0.955 \mathrm{I}_{\mathrm{d}} \mathrm{X} \mathrm{c}_{\text {c }}$ | $0.955 \mathrm{I}_{\mathrm{d}} \times \mathrm{c}$ | $0.955 \mathrm{I}_{\mathrm{d}} \mathrm{X} \mathrm{c}_{\text {c }}$ |
|  |  | 3/2 | 3 | 3 | 3 |
| PEAK MVERSE VOLTAGE |  | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es |
| $\begin{aligned} & \text { mox chest } \\ & \text { voume to } \\ & \text { anound (4) } \end{aligned}$ | + BUS GROUNDED | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es |
|  | - BUS GROUNDED | $\sqrt{2}$ Es | $\sqrt{2}$ Es | $\sqrt{2}$ Es | $\sqrt{2}$ Es |
| TOTAL <br> WINDING <br> LOSSES <br> FROM <br> TESTS | TEST Hitintis | R1-R2 | R1-R3-R5 | R1-R2, R3-R4, R5-R6 | R1-R2, R3-R4, R5-R6 |
|  | " $A$ " ${ }^{0}$ | RATED RMS CURRENT | $1.224 \times$ Rated mins Comment | RATED RMS CURRENT | RATED RMS CURRENT |
|  | TEST Mrainion iow | R3-R4 | R2-R4-R6 | R2-R3, R4-R5, R6-R1 | R2-R3, R4-R5, R6-R1 |
|  |  | RATED RMS CURRENT | $1.224 \times$ mated ras cunment | RATED RMS CURRENT | RATED RMS CURRENT |
|  | TEST Letines no |  |  | R1-R3-R5 OR R2-R4-R6 | R1-R3-R5 OR R2-R4-R6 |
|  |  |  |  | RATED RMAS CURRENT | RATED RMS CURRENT |
|  | TOTM MONDNG LOSTES FROM AEOVE TESTS (NOT <br>  | $\frac{P_{A}+P_{B}}{2}$ | $\frac{P_{A}+P_{B}}{2}$ | $\frac{P_{A}+2 P_{B}+3 P_{C}}{6}$ | $\frac{P_{A}+2 P_{B}+3 P_{C}}{6}$ |
|  |  | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 | METHOD NO. 1 |

Table 9-Rectifier circuits and properties (Continued)

| ANSI CIRCUIT NU | MBER \& NAME | DELTA, SIX PHASE <br> 23. WYE, DOUBLE WAY | WYE, SIX PHASE <br> 24. WE, DOUBLE WAY | $\begin{array}{ll}  & \text { DELTA, SIX PHASE } \\ \text { 25. } & \text { DELTA, DOUBLE WAY } \end{array}$ | WYE, SIX PHASE <br> 26. DELTA, DOUBLE WAY |
| :---: | :---: | :---: | :---: | :---: | :---: |
| NUMBER PHASES AC WINDING |  | 3 | 3 | 3 | 3 |
| NUMBER PHASES DC WDG. ( $n \times s \times \mathrm{p}=\mathrm{q}$ ) |  | 6 | 6 | 6 | 6 |
| PHASOR DUGGRAM |  | $n=1, s=2, p=3$ $\qquad$ |  |  |  |
| ANODE CURRENT | WAVE FORM |  |  |  |  |
|  | AVERAGE | $I_{d} / 3$ | $I_{d} / 3$ | $I_{d} / 3$ | $\mathrm{I}_{\mathrm{d}} / 3$ |
|  | RMS | $I_{d} / \sqrt{3}$ | $I_{d} / \sqrt{3}$ | $I_{\text {d }} / \sqrt{3}$ | $I_{d} / \sqrt{3}$ |
| D.C. WINDING CURRENT | WAVE FORM |  |  |  |  |
|  | FORM FACTOR | 1.23 | 1.23 | 1.06 | 1.06 |
|  | RMS | $\sqrt{2} I_{d} / \sqrt{3}$ | $\sqrt{2} / \sqrt{3} I_{d}$ | $\sqrt{2} / 3 I_{d}$ | $\sqrt{2} / 3 I_{d}$ |
|  | KVA RATING | $\sqrt{6} \mathrm{E}_{\mathrm{s}} \mathrm{I}_{\mathrm{d}} \times 10^{-3}$ | $\sqrt{6} E_{s} \quad I_{d} \times 10^{-3}$ | $\sqrt{6} I_{d} \quad E_{s} \times 10-3$ | $\sqrt{6} I_{d} \quad E_{s} \times 10-3$ |
| A.C. WINDING CURRENT | WAVE FORM |  |  | SAME AS <br> DC WINDING CURRENT | SAME AS <br> DC WINDING CURRENT |
|  | FORM FACTOR | 1.23 | 1.23 | 1.06 | 1.06 |
|  | RMS | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{S} / E_{L}$ | $\sqrt{2} I_{d} \times E_{s} / E_{L}$ | $\sqrt{2} / \sqrt{3} \times I_{d} \times E_{S} / E_{L}$ | $\sqrt{2} I_{d \times} E_{8} / E_{L}$ |
|  | KVA RATING | $\sqrt{6} E_{s} I_{d} \times 10^{-3}$ | SAME AS DC WNDINGS | SAME AS DC WNDINGS | SAME AS DC WNDINGS |
| A.C. LINE CURRENT | WAVE FORM |  | SAME AS <br> AC WINDING CURRENT |  | SAME AS <br> DC WINDING CURRENT |
|  | FORM FACTOR | 1.06 | 1.23 | 1.23 | 1.23 |
|  | RMS | $\sqrt{2} I_{d} E_{s} / E_{L}$ | $\sqrt{2} I_{d} E_{s} / E_{L}$ | $\sqrt{2} \quad I_{d} E_{s} / E_{L}$ | SAME AS AC WINDING |
|  | KVA RATING | $\sqrt{6}$ Es $I_{d} \times 10^{-3}$ | SAME AS DC WINDING | SAME AS DC WNDING | SAME AS DC WINDING |
| DC VOLTAGE - E do |  | $2.34 \mathrm{Es}^{\text {c }}$ | $2.34 \mathrm{Es}_{3}$ | 2.34 Es | 2.34 Es |
| DC REACTME VOLTAGE DROP E $\times$ |  | $0.955 \mathrm{I}_{\mathrm{d}} \mathrm{X}$ c | $0.955 \mathrm{I}_{d} \mathrm{X}_{\mathrm{c}}$ | $0.955 \mathrm{I}_{\mathrm{d}} \mathrm{X}_{\mathrm{c}}$ | $0.955 I_{d} X_{c}$ |
|  |  | 1 | 1 | 1 | 1 |
| PEAK INVERSE VOLTAGE |  | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
| max cresst VOLTAGE TO Ground (4) | + BUS GROUNDED | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
|  | - BUS GROUNDED | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
| TOTAL <br> WINDING <br> LOSSES <br> FROM <br> TESTS | TEST | R1-R2-R3 | R1-R2-R3 | R1-R2-R3 | R1-R2-R3 |
|  | "A" | RATED RMS CURRENT | RATED RMS CURRENT | RATED RMS CURRENT | RATED RMS CURRENT |
|  | TEST |  |  |  |  |
|  |  |  |  |  |  |
|  | TEST ${ }^{\text {Ser }}$ |  |  |  |  |
|  |  |  |  |  |  |
|  | TOTM WNONG LOSSES frow meove tests (mot Mculows interpuses) | $\mathrm{P}_{\mathrm{A}}$ | $P_{A}$ | $P_{\text {A }}$ | $\mathrm{P}_{\mathrm{A}}$ |
| TESTS AVMMABLE FOR MEASURTNG $\mathrm{X}_{\mathrm{C}} \mathrm{SEE} .8 .6$ |  | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 OR NO. 2 |

Table 9—Rectifier circuits and properties (Continued)

| ANSI CIRCUIT NUMBER \& NAME |  | delta-wre, TWELVE phase DELTA-DELTA, DOUBLE WAY | DELTA, TWELVE PHASE MULTIPLE <br> 31. DELTA-WYE, DOUBLE WAY | $\begin{aligned} & \text { DELTA TWELVE PHASE } \\ & \text { 31A DOUBLE ZIG-ZAG } \\ & \text { DOURIE WAY } \end{aligned}$ | 34 DEETA SAGX DOUBLE <br> WAY THREE-WIRE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| NUMBER PHASES AC WINDING |  | 3 | 3 | 3 | 3 |
| NUMBER PHASES DC WDG. ( $n \times s \times \mathrm{p}=\mathrm{q}$ ) |  | 12 | 12 | 12 | 6 |
| PHASOR DIAGRAM |  |  |  |  |  |
| ANODE CURRENT | WAVE FORM |  |  |  |  |
|  | AVERAGE | $I_{d / 6} / 6$ | $I_{d / 6} 6$ | $I_{d} / 6$ | $I_{d / 3}$ |
|  | RMS | I d/2 $\sqrt{3}$ | I d $/ 2 \sqrt{3}$ | $I_{d} / 2 \sqrt{3}$ | $I_{d} / \sqrt{3}$ |
| D.C. WINDING CURRENT | WAVE FORM |  |  |  |  |
|  | FORM FACTOR | 1.06 | 1.06/1.23 | 1.23 | 1.23 |
|  | RMS | $I_{d} / 3 \sqrt{2}$ | DELTA $I_{d} / 3 \sqrt{2}$ WYE $I_{d} / \sqrt{6}$ | $\mathrm{I}_{\mathrm{d}} / \sqrt{5}$ (EA. ZIG-ZAG WOG) | $\sqrt{2} / \sqrt{3} I_{d}$ |
|  | KVA RATING | $\sqrt{6} I_{d} E_{8} \times 10^{-3}$ | $\sqrt{6} I_{\text {d }} E_{s} \times 10^{-3}$ | $2.731 \mathrm{I}_{\mathrm{d}} \mathrm{Es} \times 10^{-3}$ TOTAL | $2 \sqrt{2} I_{d} E_{s} \times 10^{-3}$ |
| A.C. WINDING CURRENT | WAVE FORM |  |  |  |  |
|  | FORM FACTOR | 1.06 | 1.10 | 1.14 | 1.06 |
|  | RMS |  | $0.79 \mathrm{I}_{\mathrm{d}} \times \mathrm{E}_{s} / \mathrm{E}_{L}$ | $0.788 I_{d} E_{8} / E_{L}$ | $\sqrt{2} / \sqrt{3} I_{d} \times E_{s} / E_{L}$ |
|  | KVA RATING | SAME AS DC WINDINGS | 2.37 $I_{d}$ Es $\times 10-3$ | $2.364 I_{d}$ Es $\times 10^{-3}$ | $\sqrt{6} \bar{I}_{d} E_{s} \times 10^{-3}$ |
| A.C. LINE CURRENT | WAVE FORM |  | SAME AS <br> AC WINDING CURRENT | SAME AS <br> AC WINDING CURRENT | SAME AS <br> DC WINDING CURRENT |
|  | FORM FACTOR | 1.10 | 1.10 | 1.14 | 1.23 |
|  | RMS | $1.37 I_{d} \quad E_{s} / E_{L}$ | $1.37 \mathrm{I}_{\mathrm{d}} \quad \mathrm{E}_{s} / \mathrm{E}_{\mathrm{L}}$ | $1.365 \mathrm{I}_{\mathrm{d}} \mathrm{E}_{s} / E_{L}$ | $\sqrt{2} I_{d} E_{8} / E_{L}$ |
|  | KVA RATING | SAME AS AC WINDING | SAME AS AC WINDING | SAME AS AC WINDING | SAME AS AC WINDING |
| DC Voltage - Edo |  | $2.34 \mathrm{E}_{3}$ | 2.34 Es | 2.34 Es | $2.34 \mathrm{E}_{8}$ |
| DC REACTIVE VOLTAGE DROP E $\times$ |  | $0.478 \mathrm{I}_{\mathrm{d}} \mathrm{X}_{\mathrm{c}}$ | $0.478 \mathrm{I}_{d} \mathrm{X}_{\mathrm{c}}$ | $0.478 \mathrm{I}_{\mathrm{d}} \mathrm{X}_{c}$ | $0.955 \mathrm{I}_{d} \mathrm{X}_{\mathrm{c}}$ |
|  |  | 1 | 1 | T 1 | 1 |
| PEAK INVERSE VOLTAGE |  | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
| max CREST VOLTACE TO GROUND (4) | + BUS GROUNDED | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es | $\sqrt{6}$ Es |
|  | - BUS GROUNDED | $1.672 \sqrt{2}$ Es | $1.672 \sqrt{2}$ Es | $1.672 \sqrt{2}$ Es | $\sqrt{6} E_{8}$ (NEUT. BUS. GRO $\sqrt{2} E_{S}$ ) |
| TOTAL WINDING LOSSES FROM TESTS | TEST SHONTS | R1-R3-R5 | R1-R3-R5,R2-R4-R6 | R1-R3-R5 R2-R4-R6 | R1-R2-R3 |
|  | "A" ${ }^{\text {A }}$ | . $518 \times$ RATED RMS CURRENT | RATED RMS CURRENT | $1.036 \times$ Ratico ras Current | RATED RMS CURREN |
|  | TEST Hencrus to | R2-R4-R6 | R1-R3-R5 | R1-R3-R5 |  |
|  |  | . $518 \times$ ratid mus Current | RATED RMS CURRENT | $1.035 \times$ Ratid ras current |  |
|  | TEST SHOMNS |  | R2-R4-R6 | R2-R4-R6 |  |
|  |  |  | RATED RMS CURRENT | $1.035 \times$ rated ras Curnent |  |
|  | TOTAL WNONGG LOSSES FROM AEOVE TESTS (NOT MCLUDNG MTERPHSESS | $P_{A}+P_{B}$ | .932 $\mathrm{P}_{\mathrm{A}}+0.034\left(\mathrm{P}_{\mathrm{B}}+\mathrm{P}_{\mathrm{C}}\right)$ | $0.864 \mathrm{P}_{\mathrm{A}}+0.034\left(\mathrm{P}_{\mathrm{B}}+\mathrm{P}_{\mathrm{C}}\right)$ | $\mathrm{P}_{\mathrm{A}}$ |
| TESTS AVALAELE FOR MEASUNENG $x_{C}$ SEE 8.6 |  | METHOD NO. 1 | METHOD NO. 1 | METHOD NO. 1 | METHOD NO. 1 |

Table 9-Rectifier circuits and properties (Continued)


Table 9—Rectifier circuits and properties (Continued)

| ANSI CRECUT MUMEER \& MMME |  | 50 DETA SIX PHASE | $\begin{aligned} & \text { SOM DETA SIX PHASE } \\ & \text { PAPALE DOUBLE WE } \end{aligned}$ | 51 WTE SXX PHASE |
| :---: | :---: | :---: | :---: | :---: |
| NUMPER PHMSES AC WNOWG |  | 3 | 3 | 3 |
| NCWEER PHUSES DC WDG. ( $\mathrm{n} \times 3 \times \mathrm{p}=9$ ) |  | 6 | 6 | 6 |
| PHASOR DUGRAM |  |  |  |  |
| anoot Current | WAVE FORM |  |  |  |
|  | AVERAGE | $\mathrm{I}_{\mathrm{d}} / 12$ | $\mathrm{I}_{\mathrm{d}} / 12$ | $\mathrm{I}_{\mathrm{d}} / 12$ |
|  | RMS | $\mathrm{I}_{\mathrm{d}} / 4 \sqrt{3}$ | $\mathrm{I}_{\mathrm{d}} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ |
| D.c. WNONG CURRENT | WAVE FORM | SAME AS anode current | SAME AS anooe current | same as ANODE CURRENT |
|  | FORM FACTOR |  |  |  |
|  | RMS | $\mathrm{I}_{\mathrm{d}} / 4 \sqrt{3}$ | $I_{\text {d }} / 4 \sqrt{3}$ | $\mathrm{I}_{\mathrm{d}} / 4 \sqrt{3}$ |
|  | KVA RATNG | $\sqrt{3} \mathrm{EsI} \mathrm{I}_{\mathrm{d} \times 10^{-3}}$ | $\sqrt{3} \mathrm{Es} \mathrm{I}_{\mathrm{d}} \times 10^{10}{ }^{-3}$ | $\sqrt{3} \mathrm{Es} \mathrm{I}_{\mathrm{d} \times 1{ }^{10}{ }^{-3}}$ |
| ac. wnong CURRENT | WAvE FORM |  |  |  |
|  | FORM FACTOR | 1.23 | 1.23 | 1.23 |
|  | RMS | $\mathrm{I}_{\mathrm{d}} \sqrt{6} \quad \mathrm{E}_{8} / \mathrm{E}_{\mathrm{L}}$ | $\mathrm{I}_{\mathrm{d}} / \sqrt{\overline{8}} \quad \mathrm{E}_{\mathrm{g}} / \mathrm{E}_{\mathrm{L}}$ | $1 / \sqrt{2} \times I_{d} E_{s} / E_{L}$ |
|  | kVA RATMG | $\sqrt{3} / \sqrt{2} I_{d} E_{s} \times 10^{-3}$ | $\sqrt{3} / \sqrt{2} \mathrm{I}_{\mathrm{d}} \mathrm{E}_{8} \times 10^{-3}$ | $\sqrt{3} / \sqrt{2} \times I_{d} E_{s} \times 10^{-3}$ |
| A.C. LINE CURRENT | WAVE FORM |  |  | SAME AS <br> ac manng current |
|  | FORM FACTOR | 1.08 | 1.08 | 1.23 |
|  | RMS | $1 / \sqrt{2} I_{d} E_{8} / E_{L}$ | $1 / \sqrt{2} I_{d} E_{s} / E_{L}$ | SAME AS AC WNOWG |
|  | KVA Ratng | SMWE AS AC WNOWG | SMWE AS AC WNOWU | SAME AS AC WNOWMG |
| DC-VOLTAGE - Edo |  | 1.17 Es | 1.17 Es | 1.17 Es |
|  |  | $0.239 \mathrm{I}_{\mathrm{d}} \mathrm{C}$ c | $0.239 \mathrm{Id}_{\text {X }}$ | $0.239 \mathrm{I}_{\mathrm{d}} \times \mathrm{c}$ |
|  |  | 1 | 1 | 1 |
| PEAK MNERSE VOLTAGE |  | $2 \sqrt{2} \mathrm{Es}$ | $2 \sqrt{2} \mathrm{Es}$ | $2 \sqrt{2} \mathrm{Es}$ |
|  | + Bus crounded | $2 \sqrt{2} \mathrm{Es}$ | $2 \sqrt{2} \mathrm{Es}$ | $2 \sqrt{2} \mathrm{Es}$ |
|  | - bus grounded | $0.868 \sqrt{2} \mathrm{Es}$ | $0.866 \sqrt{2}$ Es | $0.866 \sqrt{2}$ Es |
| TOTAL <br> WINDING LOSSES FROM TESTS | IEST | R1-R3-R5 S1-S3-S5 | R1-R3-R5 S1-S3-S5 | R1-R3-R5 S1-53-S5 |
|  | " $A$ " ${ }^{\text {a }}$ | rated rms current | rated rms current | rated rms current |
|  | TEST | R2-R4-R6 S2-S4-S6 | R2-R4-R6 S2-S4-S6 | R2-R4-R6 S2-S4-S6 |
|  |  | rated rms Current | rated rus current | rated rms Current |
|  |  |  |  |  |
|  |  | $\frac{P_{A}+P_{B}}{2}$ | $\frac{P_{A}+P_{B}}{2}$ | $\frac{P_{A}+P_{B}}{2}$ |
|  |  | METHOD No. 1 OR No. 2 | METHOD No. 1 OR No. 2 | METHOD NO. 1 OR NO. 2 |

Table 9—Rectifier circuits and properties (Continued)

| ANSI CIRCUIT N | MBER \& NAME | 51A WYE, SIX PHASE PARALIE DOUBLE WYE | 52 Wre Delta, TWELVE PHASE QUADRUPLE WYE | 53 Delta, Twelve Phase QUADRUPLE ZIG-ZAG (WYE) | 53A DOUBLE DELTA 53A TWELVE PHASE QUADRUPLE ZIG-ZAG (WTE) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| NUMBER PHASES AC WINDING |  | 3 | 3 | 3 | 3 |
| NUMBER PHASES DC WDG. ( $n \times s \times p=q$ ) |  | 6 | 12 | 12 | 12 |
| PHASOR DUGRAM |  |  |  |  |  |
| ANODE CURRENT | WAVE FORM |  |  |  |  |
|  | AVERAGE | $\mathrm{I}_{\mathrm{d}} / 12$ | $\mathrm{I}_{\mathrm{d}} / 12$ | $\mathrm{I}_{\mathrm{d}} / 12$ | $I_{d / 12}$ |
|  | RLMS | $I_{d} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ |
| D.C. WINDING CURRENT | WAVE FORM | SAME AS anode current | SAME AS ANODE CURRENT | same AS ANODE CURRENT | SAME AS ANODE CURRENT |
|  | FORM FACTOR |  |  |  |  |
|  | RMS | $I_{d} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ | $I_{d} / 4 \sqrt{3}$ | $\mathrm{I}_{\mathrm{d}} / 4 \sqrt{3}$ |
|  | KVA RATING | $\sqrt{3} E_{s} I_{d} \times 10^{-3}$ | $\sqrt{3} E_{8} I_{d} \times 10^{-3}$ | $1.115 \sqrt{3} E_{8} I_{d} \times 10^{-3}$ | $1.115 \sqrt{3} E_{s} I_{d} \times 10^{-3}$ |
| A.C. WNOING CURRENT | WAVE FORM |  |  |  |  |
|  | FORM FACTOR | 1.23 | 1.23 | 1.14 | 1.10 |
|  | RMS | $1 / \sqrt{2} I_{d} E_{s} / E_{L}$ | $Y-I_{d} / 2 \sqrt{2} E_{8} / E_{L} \quad \Delta-I_{d} / 2 \sqrt{6} E_{2} / E_{L}$ | $0.394 I_{d} E_{s} / E_{L}$ | $0.204 I_{d} E_{s} / E_{L}(\mathbb{N} E A D)$ |
|  | KVA RATING | $\sqrt{3} / \sqrt{2} I_{d} \times E_{s} \times 10^{-3}$ | $(Y, \Delta) \sqrt{6} / 4 I_{d} E s \times 10^{-3}$ | $1.183 \mathrm{I}_{\mathrm{d}} \mathrm{E}_{s} \times 10^{-3}$ | $1.224 \mathrm{I}_{\mathrm{d}}$ Es $\times 10^{-3}$ |
| A.C. LINE CURRENT | WAVE FORM | SAME AS <br> AC WINDING CURRENT |  | SAME AS <br> AC WINDING CURRENT |  |
|  | FORM FACTOR | 1.23 | 1.10 | 1.14 | 1.14 |
|  | RMS | SAME AS AC WNDING | $0.684 \mathrm{I}_{\mathrm{d}} \mathrm{E}_{3} / \mathrm{E}_{\mathrm{L}}$ | $0.684 \mathrm{I}_{\mathrm{d}} \mathrm{E}_{\mathrm{s}} / \mathrm{E}_{\mathrm{L}}$ | $0.684 I_{\text {d }} E_{8} / E_{L}$ |
|  | KVA RATING | SAME AS AC WINDING | $1.183 \mathrm{I}_{\text {d }} \mathrm{E}_{\text {s }} \times 10$ | $1.183 \mathrm{I}_{\text {d }} \mathrm{E}_{s} \times 10^{-3}$ | $1.183 I_{d} E_{s} \times 10^{-}$ |
| DC VOLTAGE - E do |  | 1.17 Es | 1.17 Es | 1.17 Es | $1.17 \mathrm{E}_{3}$ |
| DC REACTIVE VOLTAGE DROP Ex |  | $0.239 \mathrm{I}_{\mathrm{d}} \mathrm{X}_{\text {c }}$ | $0.119 \mathrm{I}_{\mathrm{d}} \mathrm{Xc}_{\text {c }}$ | $0.119 \mathrm{I}_{\mathrm{d}} \mathrm{Xc}_{\mathrm{c}}$ | $0.119 \mathrm{I}_{\mathrm{d}} \mathrm{Xc}_{\text {c }}$ |
| AC UWE REACTMCETRHSFOR:ER CONSTNNTD |  | 1 | 1 | 1 | 1 |
| PEAK INVERSE VOLTAGE |  | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es |
| max crest <br> VOLTACE TO GROUND (4) | + BUS GROUNDED | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es | $2 \sqrt{2}$ Es |
|  | - BUS GROUNDED | $0.866 \sqrt{2}$ Es | $0.924 \sqrt{2}$ Es | $0.924 \sqrt{2}$ Es | $0.924 \sqrt{2}$ Es |
| TOTAL WINDING LOSSES FROM TESTS | TEST [ | R1-R3-R5 S1-S3-S5 | R1-R5-R9 R2-R6-R10 | R1-R5-R9 R2-R6-R10 | R1-R5-R9 R2-R6-R10 |
|  |  | RATED RMS CURRENT | $1.035 \times$ mated mas current | RATED RMS CURRENT | $1.036 \times$ bated ras current |
|  | TEST Yerokids to ic | R2-R4-R6 S2-S4-S6 | R3-R7-R11 R4-R8-R12 | R3-R7-R11 R4-R8-R12 | R3-R7-R11 R4-R8-R12 |
|  |  | RATED RMS CURRENT | $1.035 \times$ batid mas Current | RATED RMS CURRENT | $1.035 \times$ ratid rams Cuprent |
|  |  |  |  | TOTAL DC WNDING |  |
|  | "C" ${ }^{\text {c/ }}$ |  |  | RATED RMS CURRENT |  |
|  | TOTN MNOWG LOSSES FROM AEOVE TESTS (NOT wCluowg intrphuses) | $\frac{P_{A}+P_{B}}{2}$ | $\frac{P_{A}+P_{B}}{2}$ | $1.14 \frac{P_{A}+P_{B}}{2}-0.14 P_{C}$ | $\frac{P_{A}+P_{B}}{2}$ |
| TESTS AVAMGELE FOR MEASURMG $\mathrm{X}_{\mathrm{C}}$ SEE. 8.6 |  | METHOD NO. 1 OR NO. 2 | METHOD NO. 1 | METHOD NO. 1 | METHOD NO. 1 |

Table 10-Limits of rectifier transformer winding temperatures for defined load cycles (Temperature limits are given in a $30^{\circ} \mathrm{C}$ ambient over a 24 h period)

| Service rating class | Rated load cycle of the rectifier in \% of rated dc (see Note 1) | Limits of rectifier transformer winding temperatures |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Liquid-immersed |  | Dry-type |  |
|  |  | Insulation system, ${ }^{\circ} \mathbf{C}$ | Hottest-spot temperature (See Notes 2 \& 7), ${ }^{\circ} \mathbf{C}$ | Insulation system, ${ }^{\circ} \mathbf{C}$ | Hottest-spot temperature (See Note 7), ${ }^{\circ} \mathrm{C}$ |
| Electrochemical service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | 150 , for 1 min | See Note 3 | 140 | See Note 5 | See Note 6 |
| Industrial service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | 125 , for 2 h | See Note 3 | 140 | See Note 5 | See Note 6 |
|  | 200 , for 1 min | See Note 3 | 140 | See Note 5 | See Note 6 |
| Light traction or mining service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | 150 , for 2 h | See Note 3 | 140 | See Note 5 | See Note 6 |
|  | 200 , for 1 min | See Note 3 | 140 | See Note 5 | See Note 6 |
| Heavy traction service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | 150 , for 2 h | See Note 3 | 140 | See Note 5 | See Note 6 |
|  | 200 , for 1 min | See Note 3 | 140 | See Note 5 | See Note 6 |
| Extra-heavy traction service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | 150, for 2 h | See Note 3 | 140 | See Note 5 | See Note 6 |
|  | 300 , for 5 equally spaced periods of 1 min | See Note 3 | 140 | See Note 5 | See Note 6 |
|  | 450, for final 15 s | See Note 3 | 140 | See Note 5 | See Note 6 |
| User-defined service | 100, continuously | 120 | 110 | 150, 185, 220 | 140, 175, 210 |
|  | User-specified load | See Note 4 | 140 | See Note 4 | See Note 6 |

These are the maximum temperatures allowed. Lower temperature rises and/or higher temperature insulation systems may be specified for specific applications. Any intended overload service shall be specified to the transformer manufacturer. It is recommended that the transformer manufacturer be consulted for any overload conditions exceeding the original specification.

## NOTES TO TABLE 10

1-Current ratings in excess of $100 \%$ rated load may only be applied separately, each following the achievement of temperature conditions of operation at $100 \%$ of direct current. For purposes of defining any loss of life (see Note 3), the time period between overload applications will be assumed to be at least equal to the total time defined for loading above $100 \%$ rated load.

2-For loadings of $100 \%$ continuously, normal life expectancy will result from operating at a maximum continuous hottestspot conductor temperature of $110^{\circ} \mathrm{C}$ (or equivalent variable temperature with $120^{\circ} \mathrm{C}$ maximum) in any 24 h period.
Short-time hottest-spot temperatures above $140{ }^{\circ} \mathrm{C}$ may cause gassing in the solid insulation and liquid. This gassing may produce a potential risk to the dielectric strength integrity of the transformer. Since overloading of rectifier transformers tends to be much more frequent than for power transformers intended for more general purpose loading, conditions causing hottest-spot temperatures above $140^{\circ} \mathrm{C}$ must be avoided. (See IEEE Std C57.91-1995 for reference to above.)

3-In order to obtain satisfactory performance and life expectancy from a liquid-immersed rectifier transformer experiencing periods of overload operation, certain performance criteria must be met:
a) Maximum hottest-spot temperature must be limited to $140^{\circ} \mathrm{C}$ (See Note 2).
b) The transformer must operate "without damage" to any critical components. Several components of the transformer, such as bushings, clamps, tap switches, and leads tend to heat up quite rapidly under overload current conditions. These components may have to be selected during design with short-time overload currents in mind. The expected overload service conditions should be specified to the transformer manufacturer prior to design.
Experience has indicated that deterioration of leads, connections, and lead insulation due to excessive temperature has been one of the most common causes of failure in transformers of various manufacture.
c) The maximum calculated loss of life, during the duty cycle, must not exceed the duration of the duty cycle. This is necessary since between $110^{\circ} \mathrm{C}$ and $140^{\circ} \mathrm{C}$ hottest-spot temperatures, the rate of losing life (IEEE Std C57.91-1995) ranges from one to 21 times the nominal rate of 1 h of life $/ 1 \mathrm{~h}$ of operation. Thus a transformer that was just under the $140^{\circ} \mathrm{C}$ limit would deteriorate very quickly if it remained near that temperature for very long.
d) Loss of life calculations may be performed utilizing the loading guide for liquid-immersed transformers (IEEE Std C57.91-1995). In order to do so, however, the losses, liquid, and winding temperature rises and gradients used, must be those associated with the harmonic enhanced service conditions of rectifier operation.

## CAUTION

Care must be taken, as loading may be limited by factors other than insulation aging, such as stray flux, associated with rectifier operation or component loading. Consult the transformer manufacturer for overload capability.

4-For rectifier transformers with rated load cycles different from those above, but defined by the user, similar criteria must be used for specification and design.

When transformer user loads are of a repetitive and regular cycle pattern, the time period to be examined should be the same as a complete cycle or a maximum of 24 h .

5-In order to obtain satisfactory performance and life expectancy from a dry-type rectifier transformer experiencing periods of overload operation, certain performance criteria must be met:
a) The transformer must operate "without damage" to any critical components. Several components of the transformer, such as bus bars, core clamps, and primary levels tend to heat up quite rapidly under overload current conditions. These components may have to be selected during design with short-time overload currents in mind. Winding insulation must be limited at all times below a point of major loss of mechanical strength, melting, or fire point, etc.
b) The maximum calculated loss of life, during the duty cycle, must not exceed the duration of the duty cycle. This is necessary, since above the normal maximum hot-spot temperatures of $140^{\circ} \mathrm{C}, 175^{\circ} \mathrm{C}$, and $210^{\circ} \mathrm{C}$, respectively (dependent on the insulation system purchased), the rate of loss of life (see IEEE Std C57.96-1989) increases rapidly.
c) Loss of life calculations may be performed utilizing the loading guide for dry-type transformers (IEEE Std C57.961989). In order to do so, however, the losses, winding temperature rises, and hottest-spot temperature rises and gradients used, must be those associated with harmonic enhanced service conditions of rectifier operation.

## CAUTION

Care must be taken, as loading may be limited by factors other than insulation aging, such as stray flux, associated with rectifier operation or component loading. Consult the transformer manufacturer for overload capability.

6-For loadings of $100 \%$ continuously, normal life expectancy will result from operating at maximum continuous hot-test-spot temperatures of $140^{\circ} \mathrm{C}, 175^{\circ} \mathrm{C}$, and $210^{\circ} \mathrm{C}$ (or equivalent variable temperatures with maximums of $150^{\circ} \mathrm{C}$, $185^{\circ} \mathrm{C}$, and $220^{\circ} \mathrm{C}$, respectively) in any 24 h period.

Short-time hottest-spot temperatures above those mentioned above can be allowed, keeping due regard to the loss of life criteria. Due to the variety of dry-type insulations available, this standard cannot specify the maximum short-time limit on hottest-spot temperature above the required $150^{\circ} \mathrm{C}, 185^{\circ} \mathrm{C}$, and $220^{\circ} \mathrm{C}$ temperatures. Each manufacturer must set limiting temperatures in order to meet "without damage" criteria (see Note 5).

An rms value of overload comprising several short time periods may be used to simplify the calculation of the relative life.
Example: Extra heavy traction service: The rms load $=\left[\left(1.5^{2} \times 120+3.0^{2} \times 5+4.5^{2} \times 0.25\right) / 125.25\right]^{0.5}=1.61 \mathrm{PU}$. The 24 h normal life becomes $21 \mathrm{~h}, 54.75 \mathrm{~min}$, at 1.00 PU load plus $2 \mathrm{~h}, 5.25 \mathrm{~min}$, at 1.61 PU load.

7-Normal life expectancy as defined in the loading guides refers to a specific number of hours at rated temperature. Many transformers are fully loaded 24 hours a day for specific applications. If a user wishes to obtain 20 or more years of service, it is recommended that a lower temperature rise or auxiliary cooling be specified.

Table 11-Theoretical harmonic currents present in input current to a typical static power rectifier in PU of the fundamental current

It is the specifying engineer's responsibility to specify the harmonic content of the load current for which the transformer should be designed. However, if the actual harmonic spectrum is not known, Table 11 may be used with the full knowledge and consent of the user.

| Harmonic <br> order | Converter pulses for individual windings |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{3}$ | $\mathbf{6}$ | $\mathbf{1 2}$ | $\mathbf{1 8}$ | $\mathbf{2 4}$ |
| 2 | 0.500 |  |  |  |  |
| 4 | 0.250 |  |  |  |  |
| 5 | 0.200 | 0.200 |  |  |  |
| 7 | 0.143 | 0.143 |  |  |  |
| 8 | 0.125 |  |  |  |  |
| 10 | 0.100 |  |  |  |  |
| 11 | 0.091 | 0.091 | 0.091 |  |  |
| 13 | 0.077 | 0.077 | 0.077 |  |  |
| 14 | 0.072 |  |  |  |  |
| 16 | 0.063 |  |  |  |  |
| 17 | 0.059 | 0.059 |  | 0.059 |  |
| 19 | 0.053 | 0.053 |  | 0.053 |  |
| 20 | 0.050 |  |  |  |  |
| 22 | 0.046 |  |  |  |  |
| 23 | 0.043 | 0.043 | 0.043 |  | 0.043 |
| 25 | 0.040 | 0.040 | 0.040 |  | 0.040 |

## NOTES

1-Harmonic orders are determined by the harmonic composition law:

$$
n q \pm 1
$$

where $n$ is any integer and $q$ is the converter pulse.
The amplitude of the harmonic current in per unit value is $1 / h$.
The cut-off point of the 25th harmonic is reasonable since the full theoretical magnitude of PU fundamental harmonic current is used above. This should yield a conservative estimate of harmonic currents for most applications.
2-Appropriate harmonics for the pulses affecting a winding must be used. For example, a tightly coupled circuit 45 transformer should consider the primary winding as a six-pulse winding, while the secondary windings should be considered as a three-pulse winding, with the appropriate leakage field cancellation considered.

## Annex A

(informative)

## Harmonic loss calculation examples

## A. 1 Determination of transformer load losses under distorted load current

Listed below are several examples of load-loss calculations for transformers when subjected to nonsinusoidal currents. These are based on calculations in 8.6.

Example 1. This is an example of a two-winding transformer. It is a six-pulse motor-drive transformer.

Table A.11-2700 kVA (fundamental), dry-type transformer, 150 rise, aluminum windings

| Transformer rating | Primary <br> winding | Secondary <br> winding |
| :--- | :---: | :---: |
| Rated power (fundamental) | 2700 | 2700 |
| Rated power (rms) | 2782 | 2782 |
| Rated system voltage (V) | 4160 | 1000 |
| Rated fundamental line current (A) | 374.72 | 1558.85 |
| Connection | Delta | Wye |

Test results are based on 2700 kVA fundamental rating, rated voltage, 60 Hz , and with losses corrected to 170 C .

Measured resistance (ohms/phase) corrected to 170 C :

| Primary winding | 0.100000 |
| :--- | ---: |
| Secondary winding | 0.001631 |
| Measured impedance | $6.18 \%$ |
| Tested core loss | 5328 W |
| Tested load loss | 28452 W |
| Tested total loss | 33780 W |

As this is a two-winding transformer, both windings are subject to the same harmonic spectrum. This is not generally true of multiwinding transformers.

The transformer is subjected to the load current harmonic spectrum in Table A.2. PU values are based on the fundamental current.

Table A.12—Load current harmonic spectrum for two-winding transformer

| Harmonic order | PU load current |
| :---: | :---: |
| 1 | 1.000 |
| 5 | 0.190 |
| 7 | 0.130 |
| 11 | 0.070 |
| 13 | 0.050 |
| 17 | 0.030 |
| 19 | 0.020 |
| 23 | 0.010 |
| 25 | 0.005 |

The harmonic loss factors are calculated in Table A. 3 with the values from Table A.2.

Table A.13-Harmonic loss factors for two-winding transformer

| Harmonic order (h) | Fundamental (PU-A) | $\underset{(\mathbf{P U}-\mathbf{A})^{2}}{\text { Fundamental }}$ | $F_{\text {HL-WE }}$ | $\boldsymbol{F}_{\text {HL-OSL }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1.0000 | 1.000000 | 1.0000 | 1.0000 |
| 5 | 0.1900 | 0.036100 | 0.9025 | 0.1308 |
| 7 | 0.1300 | 0.916900 | 0.8281 | 0.0802 |
| 11 | 0.0700 | 0.004900 | 0.5929 | 0.0334 |
| 13 | 0.0500 | 0.002500 | 0.4225 | 0.0195 |
| 17 | 0.0300 | 0.000900 | 0.2601 | 0.0087 |
| 19 | 0.0200 | 0.000400 | 0.1444 | 0.0042 |
| 23 | 0.0100 | 0.000100 | 0.0529 | 0.0012 |
| 25 | 0.0050 | 0.000025 | 0.0156 | 0.0003 |
|  |  | $\Sigma 1.0618$ | 4.2190 | 1.2783 |
| RMS PU current: |  | 1.0304 |  |  |

Verifying the $\mathrm{rms} \mathrm{kVA}=1.0304 \times 2700 \mathrm{kVA}=2782 \mathrm{kVA}$.
Measured dc resistance load loss at $170 \mathrm{C}, 60 \mathrm{~Hz}$, and rated fundamental current:
$I_{\mathrm{p} 1}=374.72 \mathrm{~A}$ and $I_{\mathrm{s} 1}=1558.85 \mathrm{~A}$
Primary winding $I^{2} R=3 \times(216.34 \mathrm{~A})^{2} \times 0.100000 \Omega \quad=14041 \mathrm{~W}$
Secondary winding $I^{2} R=3 \times(1558.85 \mathrm{~A})^{2} \times 0.001631 \Omega \quad=11890 \mathrm{~W}$
Total dc resistance load loss $=25931 \mathrm{~W}$

Calculated winding eddy current losses at 170 C :

| Primary windings | $=447 \mathrm{~W}$ |
| :--- | :--- |
| Secondary windings | $=1644 \mathrm{~W}$ |
| Total windings | $=2091 \mathrm{~W}$ |

Total stray and winding eddy current loss $=28452 \mathrm{~W}-25931 \mathrm{~W}$

$$
\begin{aligned}
= & 2521 \mathrm{~W} \\
& =430 \mathrm{~W}
\end{aligned}
$$

Total other stray loss, $P_{\text {OSL }}=2521 \mathrm{~W}-2091 \mathrm{~W}$
The total service $I^{2} R$ loss is the fundamental $I^{2} R \operatorname{loss} \times\left(I_{\mathrm{rms}} / I_{1}\right)^{2}$;
The service winding eddy current loss is the fundamental eddy loss $\times F_{\mathrm{HL}-\mathrm{WE}}$;
The service other stray loss is the fundamental other stray loss $\times F_{\mathrm{HL}-\mathrm{OSL}}$.
Primary service $I^{2} R$ loss $=14041 \mathrm{~W} \times 1.0304^{2}=14908 \mathrm{~W}$
Primary service winding eddy current loss, $P^{\prime}{ }_{\text {EC-P }}=447 \mathrm{~W} \times 4.2190 \quad=1886 \mathrm{~W}$
Total primary winding service loss, $P_{\text {R-P }} \quad=16794 \mathrm{~W}$
Secondary service $I^{2} R$ loss $=11890 \mathrm{~W} \times 1.0304^{2} \quad=12624 \mathrm{~W}$
Secondary winding eddy current loss, $P_{\text {EC-S }}^{\prime}=1644 \mathrm{~W} \times 4.2190=6936 \mathrm{~W}$
Total secondary winding service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}$
$=19560 \mathrm{~W}$

Service other stray loss, $P^{\prime}$ osL $=430 \mathrm{~W} \times 1.2783=550 \mathrm{~W}$
Total service load loss for the transformer with distorted load current, $P_{\text {OSL }}^{\prime}=16794 \mathrm{~W}+19560 \mathrm{~W}+550 \mathrm{~W}=36904 \mathrm{~W}$

To obtain the total service loss, add the tested core loss to total service load loss calculated above.
Total service loss, $P^{\prime}$ тOTAL $=5328 \mathrm{~W}+36904 \mathrm{~W}$ $=42232 \mathrm{~W}$

## A. 2 Three-winding transformer loss calculations

Example 1 is a simple two-winding transformer where the harmonic loss factor is the same for both the primary and secondary windings. This is not the case for three-winding or higher transformers. Knowledge of the winding construction, secondary coupling, and harmonic loss factors is necessary. A rigorous Fourier Analysis is required to predict harmonic loss factors to great accuracy. Some assumptions, which are generally conservative and easier mathematically, may be made.

Windings that have two coils, with coil currents that have even harmonic currents, but are connected in phase opposition, have cancellation of all even harmonic fluxes. Single-way transformers with two wye secondaries connected in $180^{\circ}$ opposition, such as ANSI circuit 45 or 46 , are an example. The coil current is rich in even harmonics. The fluxes due to the even harmonic currents are cancelled, leaving the normal odd harmonic fluxes (5th, 7th, 11th, 13th, etc.). The secondaries of these transformers are tightly coupled; otherwise the cancellation of even harmonics would not occur in the windings. It is important to note that the fluxes due to the harmonics are cancelled while the currents are still carried by the windings. If these windings are not tightly coupled, the eddy losses may be unmanageable. For tightly coupled windings, rather than performing the rigorous Fourier Analysis, it can generally be assumed that while the even harmonic fluxes are essentially cancelled, the odd harmonic fluxes are the same. This is all due to flux field cancellation. A more rigorous complete Fourier Analysis may be performed if desired. The even harmonic currents and fluxes are both cancelled in the primary winding. Example number 2 is this type of transformer.

A similar argument can be made for ANSI circuit 31 transformers. These transformers may be tightly coupled, loosely coupled, or somewhere in between due to construction economics, short-circuit characteristics, or desired voltage regulation. ANSI circuit 31 is a 12-pulse double-way with a delta and wye secondary with
$30^{\circ}$ coupling due to the phase displacement in the windings. Also, the primary winding may be a single common primary, or two paralleled windings.

If a circuit 31 transformer is wound with a single common primary and tightly coupled secondaries, the flux caused by the 5th and 7th harmonic currents and multiples cancel in the secondary windings, while the secondary windings still carry the 5th and 7th harmonic currents, as well as their multiples. For tightly coupled windings, rather than performing the rigorous Fourier Analysis, we can generally assume that while the 5th and 7th harmonic fluxes and their multiples are essentially cancelled, the 11th and 13th harmonic fluxes and their multiples are the same. This is all due to flux field cancellation. A more rigorous complete Fourier Analysis may be performed if desired. The 5th and 7th harmonic currents and fluxes both cancel in the primary windings. Example number 3 is this type of transformer.

If a circuit 31 transformer is wound with loosely coupled secondaries, but with a common primary, a different effect is found. Completely noncoupled secondaries generally do not occur on a common core, with coupling from 10 to $20 \%$ common. In general, however, the approach is to ignore the small amount of secondary coupling and provide no harmonic flux or current cancellation in the calculations for the secondary windings. The primary winding has flux and current cancellation for the 5th and 7th harmonics, as well as their multiples.

If a circuit 31 transformer has loosely coupled secondaries, with paralleled primary windings, little harmonic cancellation effect is found. While rigorous Fourier Analysis may be performed, in general, both secondary windings and primary windings are subjected to the full six-pulse harmonics with no correction required. The harmonic current and flux cancellation of the 5th and 7th harmonics and their multiples occurs only at the terminals of the transformer. While the power supply may be cleaner, the transformer design must provide cooling for all of the harmonic effects of a six-pulse design. Example 4 is this type of transformer.

Example 2. This is an example of a three-winding transformer. It is a six-pulse single-way electrochemical service application, ANSI circuit 46. This example uses a rigorous Fourier Analysis to determine all ratings and harmonic loss factors.

Table A.4-17 $\mathbf{6 4 0}$ kVA (fundamental), liquid-immersed transformer, 55 rise, copper windings, 50 Hz

| Transformer rating | Primary <br> winding | Secondary <br> winding $\mathbf{1}$ | Secondary <br> winding 2 |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Rated power (fundamental) | 17640 | 8820 | 8820 |  |  |
| Rated power (rms) | 18069 | 12770 | 12770 |  |  |
| Rated system voltage (V) | 30000 | $\sqrt{3} \times 303$ | $\sqrt{3} \times 303$ |  |  |
| Rated fundamental line current (A) | Wye | Wye | Wye |  |  |
| Connection |  |  |  |  |  |
| With interphase transformer in common tank. <br> Convertor rating: $E_{\mathrm{d}}=320 \mathrm{~V}, E_{\mathrm{d} 0}=354 \mathrm{~V}, I_{\mathrm{d}}=50000 \mathrm{~A}$ |  |  |  |  |  |

Test results are based on 17640 kVA fundamental rating, rated voltage, 50 Hz , and with losses corrected to 75 C.

Tested resistance (ohms/phase) for three-winding transformer corrected to 75 C :

| Primary winding | $88.90 \times 10^{-3}$ |
| :--- | ---: |
| Secondary winding 1 | $53.5 \times 10^{-6}$ |
| Secondary winding 2 | $53.8 \times 10^{-6}$ |
| Interphase leg 1 | $17.9 \times 10^{-6}$ |
| Interphase leg 2 | $16.5 \times 10^{-6}$ |
| Main core loss | 20454 W |
| Interphase core loss | 4125 W |

As this is a tightly coupled secondary winding transformer, both windings are subject to essentially the same harmonic spectrum with regard to field flux. This is not always true of multiwinding transformers.

The transformer is subjected to the load current harmonic spectrum in Table A.5. PU values are based on the fundamental current.

Table A.5-Load current harmonic spectrum for three-winding transformer

| Harmonic order | PU load current secondary | PU flux secondary | PU load current and flux-primary |
| :---: | :---: | :---: | :---: |
| dc | 0.858 | 0 | 0 |
| 1 | 1.000 | 1.000 | 1.000 |
| 2 | 0.493 | 0 | 0 |
| 4 | 0.233 | 0 | 0 |
| 5 | 0.179 | 0.179 | 0.179 |
| 7 | 0.114 | 0.114 | 0.114 |
| 8 | 0.093 | 0 | 0 |
| 10 | 0.062 | 0 | 0 |
| 11 | 0.050 | 0.050 | 0.050 |
| 13 | 0.033 | 0.033 | 0.033 |
| 14 | 0.027 | 0 | 0 |
| 16 | 0.018 | 0 | 0 |
| 17 | 0.015 | 0.015 | 0.015 |
| 19 | 0.012 | 0.012 | 0.012 |
| 20 | 0.011 | 0 | 0 |
| 22 | 0.010 | 0 | 0 |
| 23 | 0.009 | 0.009 | 0.009 |
| 25 | 0.008 | 0.008 | 0.008 |
| Secondary rms PU current: 1.4479 |  |  |  |

The harmonic loss factors are calculated in Table A. 6 with the values from Table A.5.

Table A.6-Harmonic loss factors for three-winding transformer

| Harmonic <br> order $(\boldsymbol{h})$ | Fundamental <br> $(\mathbf{P U}-\mathbf{A})$ | Fundamental <br> $(\mathbf{P U}-\mathbf{A})^{2}$ | $\boldsymbol{F}_{\text {HL-WE }}$ | $\boldsymbol{F}_{\text {HL-OSL }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 5 | 0.1790 | 0.0320 | 0.8010 | 0.1161 |
| 7 | 0.1140 | 0.0130 | 0.6368 | 0.0616 |
| 11 | 0.0500 | 0.0025 | 0.3025 | 0.0170 |
| 13 | 0.0330 | 0.0011 | 0.1840 | 0.0085 |
| 17 | 0.0150 | 0.0002 | 0.0650 | 0.0022 |
| 19 | 0.0120 | 0.0001 | 0.0520 | 0.0015 |
| 23 | 0.0090 | 0.0001 | 0.0428 | 0.0010 |
| 25 | 0.0080 | 0.0001 | 0.0400 | 0.0008 |
| Primary rms PU current: | 1.0243 | 1.0491 | 3.1242 | 1.2088 |
| $\quad \Sigma$ |  |  |  |  |

Verifying the primary rms kVA $=1.0243 \times 17640 \mathrm{kVA}=18069 \mathrm{kVA}$.
Verifying the secondary $\mathrm{rms} \mathrm{kVA}=1.4479 \times 8820 \mathrm{kVA}=12770 \mathrm{kVA}$.

Note that during the loss tests and measurements, each secondary winding will be tested with $\sqrt{2}$ more current than its fundamental rating. The calculations must therefore introduce the same $\sqrt{2}$ factor as a multiplier of the fundamental current. If this is not done, the values of stray loss yielded from the tests will be too high. The secondary rms PU current factor above yields a value of 1.4479 . The ratio of these two values is $1.4479 / \sqrt{2}=1.0238$.

Measured dc resistance load loss at $75 \mathrm{C}, 50 \mathrm{~Hz}$, and rated fundamental current:
$I_{\mathrm{p} 1}=339.5 \mathrm{~A}$ and $I_{\mathrm{s} 1}=I_{\mathrm{s} 2}=\sqrt{2} \times 9700.0 \mathrm{~A}=13717.9 \mathrm{~A}$.
Primary winding $I^{2} R=3 \times(339.5 \mathrm{~A})^{2} \times 88.9 \times 10^{-3} \Omega$
Secondary winding $1=I^{2} R=3 \times(13717.9 \mathrm{~A})^{2} \times 53.5 \times 10^{-6} \Omega$

$$
\begin{aligned}
& =30740 \mathrm{~W} \\
& =30203 \mathrm{~W} \\
& =30372 \mathrm{~W} \\
& =91315 \mathrm{~W}
\end{aligned}
$$

Secondary winding $2=I^{2} R=3 \times(13717.9 \mathrm{~A})^{2} \times 53.8 \times 10^{-6} \Omega$
Total dc resistance load loss

Total measured main fundamental load losses at 75 C

$$
=118564 \mathrm{~W}
$$

Calculated fundamental winding eddy current losses at 75 C :

$$
\begin{array}{lr}
\text { Primary windings } & =340 \mathrm{~W} \\
\text { Each secondary winding } & =1450 \mathrm{~W} \\
\text { Total windings } & =3240 \mathrm{~W}
\end{array}
$$

Total stray and winding eddy current loss $=118564 \mathrm{~W}-91315 \mathrm{~W}=27249 \mathrm{~W}$
Total other stray loss, $P_{\text {OSL }}=27249 \mathrm{~W}-3240 \mathrm{~W}$ $=24009 \mathrm{~W}$

The total service $I^{2} R$ loss is the fundamental $I^{2} R \operatorname{loss} \times\left(I_{\mathrm{rms}} / I_{1}\right)^{2}$;
The service winding eddy current loss is the fundamental eddy loss $\times F_{\mathrm{HL}-\mathrm{WE}}$;
The service other stray loss is the fundamental other stray loss $\times F_{\mathrm{HL}-\mathrm{OSL}}$.
Primary service $I^{2} R$ loss $=30740 \mathrm{~W} \times 1.0243^{2} \quad=32252 \mathrm{~W}$
Primary service winding eddy current loss, $P_{\text {EC-P }}^{\prime}=340 \mathrm{~W} \times 3.1242=1062 \mathrm{~W}$
Total primary winding service loss, $P_{\mathrm{R}-\mathrm{P}}$
$=33314 \mathrm{~W}$
Secondary 1 service $I^{2} R$ loss $=30203 \mathrm{~W} \times 1.0238^{2}$
$=31658 \mathrm{~W}$
Secondary winding eddy current loss, $P^{\prime}{ }_{\text {EC-S }}=1450 \mathrm{~W} \times 3.1242$ $=4530 \mathrm{~W}$
Total secondary winding 1 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}=$ 36188 W

Secondary 2 service $I^{2} R$ loss $=30372 \mathrm{~W} \times 1.0238^{2}=$
31836 W
Secondary winding eddy current loss, $P^{\prime}{ }_{\text {EC-S }}=1450 \mathrm{~W} \times 3.1242$ $=4530 \mathrm{~W}$
Total secondary winding 2 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}=$ 36366 W

Service other stray loss, $P^{\prime}{ }_{\text {osL }}=24009 \mathrm{~W} \times 1.2088=$ 29022 W
Total service load loss for the main transformer with distorted load current,
$P^{\prime}{ }_{\mathrm{R}-\mathrm{m}}=33314 \mathrm{~W}+36188 \mathrm{~W}+36366 \mathrm{~W}+29022 \mathrm{~W}$
$=34890 \mathrm{~W}$

Interphase transformer load loss $=(25000 \mathrm{~A})^{2} \times(17.9+16.5) \times 10^{-6}$
$=21500 \mathrm{~W}$

Total service load loss for the total transformer with distorted load current,

$$
P_{\mathrm{R}}^{\prime}=134890 \mathrm{~W}+21500 \mathrm{~W} \quad=156390 \mathrm{~W}
$$

To obtain the total service loss, add the tested core losses to total service load loss calculated above.
Total service loss, $P^{\prime}$ тотад $=20454 \mathrm{~W}+4125 \mathrm{~W}+156390 \mathrm{~W}=180969 \mathrm{~W}$
It is interesting to note that the fundamental kVA ratings of the secondaries added together equal the fundamental primary kVA. However, the rms kVA ratings of the secondaries added together equal $\sqrt{2}$ times the primary kVA as always for this circuit.

Example 3. Twelve-pulse double-way with tightly coupled secondaries, ANSI circuit 31.

Table A.7-8830 kVA (fundamental), liquid-immersed transformer, 55 rise, copper windings, 60 Hz , for electrochemical service

| Transformer rating | Primary <br> winding | Secondary <br> winding 1 | Secondary <br> winding 2 |
| :--- | :---: | :---: | :---: |
| Rated power (fundamental) | 8830 | 4415 | 4415 |
| Rated power (rms) | 8843 | 4515 | 4515 |
| Rated system voltage (V) | 20000 | 208.2 | 208.2 |
| Rated fundamental line current (A) | 254.90 | 12243 | 12243 |
| Connection | Delta | Delta | Wye |
| Convertor rating: $E_{\mathrm{d}}=250 \mathrm{~V}, E_{\mathrm{d} 0}=281 \mathrm{~V}$, and $I_{\mathrm{d}}=31000 \mathrm{~A}$. |  |  |  |

Test results are based on 8830 kVA fundamental rating, rated voltage, 60 Hz , and with losses corrected to 75 C.

Tested resistance (ohms/phase) corrected to 75 C :
Primary winding
$431.97 \times 10^{-3}$
Secondary winding 1
$114.75 \times 10^{-6}$
Secondary winding 2 $37.95 \times 10^{-6}$
Core loss 6080 W

As this is a tightly coupled secondary winding transformer, both windings are subject to essentially the same harmonic spectrum with regard to field flux. This is not always true of multiwinding transformers.

The transformer is subjected to the load current harmonic spectrum in Table A.8. PU values are based on the fundamental current.

## Table A.8-Load current harmonic spectrum for tightly coupled secondary winding transformer

| Harmonic order | PU load current <br> secondary | PU flux secondary | PU load current and <br> flux-primary |
| :---: | :---: | :---: | :---: |
| 1 | 1.000 | 1.000 | 1.000 |
| 5 | 0.175 | 0 | 0 |
| 7 | 0.110 | 0 | 0 |
| 11 | 0.045 | 0.045 | 0.045 |
| 13 | 0.029 | 0.029 | 0.029 |
| 17 | 0.015 | 0 | 0 |
| 19 | 0.010 | 0 | 0 |
| 23 | 0.007 | 0.007 | 0.007 |
| 25 | 0.006 | 0.006 | 0.006 |
| Secondary rms PU current $=1.0227$. |  |  |  |
| Primary rms PU current $=1.0015$. |  |  |  |

The harmonic loss factors are calculated in Table A. 9 with the values from Table A.8.

Table A.9—Harmonic loss factors for tightly coupled
secondary winding transformer

| Harmonic <br> order $(\boldsymbol{h})$ | Fundamental <br> $(\mathbf{P U}-\mathbf{A})$ | Primary <br> $\boldsymbol{F}_{\text {HL-WE }}$ | Secondary <br> $\boldsymbol{F}_{\text {HL-WE }}$ | $\boldsymbol{F}_{\text {HL-OSL }}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 5 | 0.1750 | 0.0000 | 0.0000 | 0.1110 |
| 7 | 0.1100 | 0.0000 | 0.0000 | 0.0574 |
| 11 | 0.0450 | 0.2450 | 0.2450 | 0.0138 |
| 13 | 0.0290 | 0.1421 | 0.1421 | 0.0065 |
| 17 | 0.0150 | 0.0000 | 0.0000 | 0.0022 |
| 19 | 0.0100 | 0.0000 | 0.0000 | 0.0011 |
| 23 | 0.0070 | 0.0259 | 0.0259 | 0.0006 |
| 25 | 0.0060 | 0.0225 | 0.0225 | 0.0005 |
|  | $\Sigma 1.4356$ | 1.4356 | 1.1930 |  |

Verifying the primary $\mathrm{rms} \mathrm{kVA}=1.0015 \times 8830 \mathrm{kVA}=8843 \mathrm{kVA}$.
Verifying the secondary $\mathrm{rms} \mathrm{kVA}=1.0227 \times 4415 \mathrm{kVA}=4515 \mathrm{kVA}$ each.
Measured dc resistance load loss at $75 \mathrm{C}, 60 \mathrm{~Hz}$, and rated fundamental current:
$I_{\mathrm{p} 1}=254.90 \mathrm{~A}$ and $I_{\mathrm{s} 1}=I_{\mathrm{s} 2}=12243 \mathrm{~A}$
Primary winding $I^{2} R=3 \times(147.17 \mathrm{~A})^{2} \times 431.97 \times 10^{-3} \Omega \quad=28068 \mathrm{~W}$
Secondary winding $1=I^{2} R=3 \times(7068.5 \mathrm{~A})^{2} \times 114.75 \times 10^{-6} \Omega \quad=17200 \mathrm{~W}$
Secondary winding $2=I^{2} R=3 \times(12243 \mathrm{~A})^{2} \times 37.95 \times 10^{-6} \Omega \quad=17065 \mathrm{~W}$
Total dc resistance load loss
$=62333 \mathrm{~W}$
Total measured main fundamental load losses at 75 C
$=75508 \mathrm{~W}$

Calculated fundamental winding eddy current losses at 75 C :
Primary winding

$$
=540 \mathrm{~W}
$$

Secondary winding 1
$=1250 \mathrm{~W}$
Secondary winding 2
$=1867 \mathrm{~W}$
Total windings

$$
=3657 \mathrm{~W}
$$

Total stray and winding eddy current loss $=75508 \mathrm{~W}-62333 \mathrm{~W}$ $=13175 \mathrm{~W}$

Total other stray loss, $P_{\mathrm{OSL}}=13175 \mathrm{~W}-3657 \mathrm{~W}$

$$
=9518 \mathrm{~W}
$$

The total service $I^{2} R$ loss is the fundamental $I^{2} R \operatorname{loss} \times\left(I_{\mathrm{rms}} / I_{1}\right)^{2}$;
The service winding eddy current loss is the fundamental eddy loss $\times F_{\mathrm{HL}-\mathrm{WE}}$;
The service other stray loss is the fundamental other stray loss $\times F_{\text {HL-OSL }}$.
Primary service $I^{2} R$ loss $=28068 \mathrm{~W} \times 1.0015^{2}=28152 \mathrm{~W}$

Primary service winding eddy current loss, $P^{\prime}{ }_{\text {EC-P }}=540 \mathrm{~W} \times 1.4356$
Total primary winding service loss, $P_{\mathrm{R}-\mathrm{P}}$
Secondary 1 service $I^{2} R$ loss $=17200 \mathrm{~W} \times 1.0227^{2}$
Secondary winding eddy current loss, $P_{\text {EC-S }}^{\prime}=1250 \mathrm{~W} \times 1.4356$
Total secondary winding 1 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}$
Secondary 2 service $I^{2} R$ loss $=17065 \mathrm{~W} \times 1.0227^{2}$
Secondary winding eddy current loss, $P_{\text {EC-S }}^{\prime}=1867 \mathrm{~W} \times 1.4356$
Total secondary winding 2 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}$
Service other stray loss, $P^{\prime}$ osL $=9518 \mathrm{~W} \times 1.1930$
Total service load loss for the transformer with distorted load current,
$P_{R}^{\prime}=28927 \mathrm{~W}+19785 \mathrm{~W}+20529 \mathrm{~W}+11355 \mathrm{~W}$

$$
\begin{array}{r}
=775 \mathrm{~W} \\
=28927 \mathrm{~W} \\
=17990 \mathrm{~W} \\
=1795 \mathrm{~W} \\
=19785 \mathrm{~W} \\
=17849 \mathrm{~W} \\
=2680 \mathrm{~W} \\
=20529 \mathrm{~W} \\
=11355 \mathrm{~W} \\
=80596 \mathrm{~W}
\end{array}
$$

To obtain the total service loss, add the tested core losses to total service load loss calculated above
Total service loss, $P^{\prime}{ }_{\text {тотаL }}=80596 \mathrm{~W}+6080 \mathrm{~W}=86676 \mathrm{~W}$
Example 4. Twelve-pulse double-way with loosely coupled secondaries, ANSI circuit 31. This construction has two paralleled primary windings. One set of primaries and secondaries is stacked above the other on the same core leg. There is minor coupling, but it may be ignored.

Table A. 10-15 000 kVA (fundamental), liquid-immersed transformer, 55 rise, copper windings, 60 Hz , for adjustable speed drive service

| Transformer rating | Primary winding | Secondary <br> winding 1 | Secondary <br> winding 2 |
| :--- | :---: | :---: | :---: |
| Rated power (fundamental) | 7500 each | 7500 | 7500 |
| Rated power (rms) | 7670 each | 7670 | 7670 |
| Rated system voltage (V) | 12000 | 4400 | 4400 |
| Rated fundamental line current (A) | 360.84 each | 984.12 | 984.12 |
| Connection | Delta | Delta | Wye |

Test results are based on 15000 kVA fundamental rating, rated voltage, 60 Hz , and with losses corrected to 75 C.

Tested resistance (ohms/phase) corrected to 75 C :

| Primary winding 1 | $121.37 \times 10^{-3}$ |
| :--- | ---: |
| Primary winding 2 | $122.77 \times 10^{-3}$ |
| Secondary winding 1 | $12.42 \times 10^{-3}$ |
| Secondary winding 2 | $4.13 \times 10^{-3}$ |
| Core loss | 21700 W |

As this is a loosely coupled secondary winding transformer, both windings are subject to essentially the same harmonic spectrum with regard to both field flux and load current. This is not always true of multiwinding transformers.

The transformer is subjected to the load current harmonic spectrum in Table A.11. PU values are based on the fundamental current.

Table A.11-Load current harmonic spectrum for twelve-pulse, double-way transformers, with loosely coupled secondaries

| Harmonic order | PU load current <br> secondary | PU flux secondary | PU load current and <br> flux-primary |
| :---: | :---: | :---: | :---: |
| 1 | 1.000 | 1.000 | 1.000 |
| 5 | 0.175 | 0.175 | 0.175 |
| 7 | 0.110 | 0.110 | 0.110 |
| 11 | 0.045 | 0.045 | 0.045 |
| 13 | 0.029 | 0.029 | 0.029 |
| 17 | 0.015 | 0.015 | 0.015 |
| 19 | 0.010 | 0.010 | 0.010 |
| 23 | 0.007 | 0.007 | 0.007 |
| 25 | 0.006 | 0.006 | 0.006 |
| Secondary rms PU current $=1.0227$ |  |  |  |
| Primary rms PU current $=1.0227$ |  |  |  |

The harmonic loss factors are calculated in Table A. 12 with the values from Table A.11.

Table A.12—Harmonic loss factors for tightly coupled secondary winding transformer

| Harmonic <br> order $(\boldsymbol{h})$ | Fundamental <br> $(\mathbf{P U}-\mathbf{A})$ | Primary <br> $\boldsymbol{F}_{\text {HL-WE }}$ | Secondary <br> $\boldsymbol{F}_{\text {HL-WE }}$ | $\boldsymbol{F}_{\text {HL-OSL }}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |  |  |  |
| 5 | 0.1750 | 0.7656 | 0.7656 | 0.1110 |  |  |  |
| 7 | 0.1100 | 0.5929 | 0.5929 | 0.0574 |  |  |  |
| 11 | 0.0450 | 0.2450 | 0.2450 | 0.0138 |  |  |  |
| 13 | 0.0290 | 0.1421 | 0.1421 | 0.0065 |  |  |  |
| 17 | 0.0150 | 0.0650 | 0.0650 | 0.0022 |  |  |  |
| 19 | 0.0100 | 0.0361 | 0.0361 | 0.0011 |  |  |  |
| 23 | 0.0070 | 0.0259 | 0.0259 | 0.0006 |  |  |  |
| 25 | 0.0060 | 0.0225 | 0.0225 | 0.0005 |  |  |  |
|  | 2.8952 |  |  |  |  | 2.8952 | 1.1930 |

Verifying the primary $\mathrm{rms} \mathrm{kVA}=1.0227 \times 7500 \mathrm{kVA}=7670 \mathrm{kVA}$ each.

Verifying the secondary $\mathrm{rms} \mathrm{kVA}=1.0227 \times 7500 \mathrm{kVA}=7670 \mathrm{kVA}$ each.
Measured dc resistance load loss at $75 \mathrm{C}, 60 \mathrm{~Hz}$, and rated fundamental current:
$I_{\mathrm{p} 1}=360.84 \mathrm{~A}$ each and $I_{\mathrm{s} 1}=I_{\mathrm{s} 2}=984.12 \mathrm{~A}$
Primary winding $1 I^{2} R=3 \times(208.33 \mathrm{~A})^{2} \times 121.37 \times 10^{-3} \Omega=15803 \mathrm{~W}$
Primary winding $2 I^{2} R=3 \times(208.33 \mathrm{~A})^{2} \times 122.77 \times 10^{-3} \Omega \quad=15985 \mathrm{~W}$
Secondary winding $1=I^{2} R=3 \times(568.18 \mathrm{~A})^{2} \times 12.42 \times 10^{-3} \Omega \quad=12026 \mathrm{~W}$
Secondary winding $2=I^{2} R=3 \times(984.12 \mathrm{~A})^{2} \times 4.13 \times 10^{-3} \Omega \quad=12000 \mathrm{~W}$
Total dc resistance load loss
$=55814 \mathrm{~W}$

Total measured main fundamental load losses at $75 \mathrm{C}=63518 \mathrm{~W}$

Calculated fundamental winding eddy current losses at 75 C :

| Primary winding 1 | $=240 \mathrm{~W}$ |
| :--- | ---: |
| Primary winding 2 | $=240 \mathrm{~W}$ |
| Secondary winding 1 | $=850 \mathrm{~W}$ |
| Secondary winding 2 | $=1267 \mathrm{~W}$ |
| Total windings | $=2597 \mathrm{~W}$ |

Total stray and winding eddy current loss $=63518 \mathrm{~W}-55814 \mathrm{~W}=7704 \mathrm{~W}$
Total other stray loss, $P_{\text {OSL }}=7704 \mathrm{~W}-2597 \mathrm{~W}=5107 \mathrm{~W}$
The total service $I^{2} R$ loss is the fundamental $I^{2} R \operatorname{loss} \times\left(I_{\mathrm{rms}} / I_{1}\right)^{2}$;
The service winding eddy current loss is the fundamental eddy loss $\times F_{\mathrm{HL}-\mathrm{WE}}$;
The service other stray loss is the fundamental other stray loss $\times F_{\mathrm{HL}-\mathrm{OSL}}$.
Primary 1 service $I^{2} R$ loss $=15803 \mathrm{~W} \times 1.0227^{2}$
$=16529 \mathrm{~W}$
Primary 1 service winding eddy current loss, $P^{\prime}{ }_{\text {EC-P }}=240 \mathrm{~W} \times 2.8952$ $=695 \mathrm{~W}$
Total primary 1 winding service loss, $P_{\text {R-P }}$
$=17224 \mathrm{~W}$
Primary 2 service $I^{2} R$ loss $=15985 \mathrm{~W} \times 1.0227^{2}$
$=16719 \mathrm{~W}$
Primary 2 service winding eddy current loss, $P_{\text {EC-P }}^{\prime}=240 \mathrm{~W} \times 2.8952$ $=695 \mathrm{~W}$
Total primary 2 winding service loss, $P_{\mathrm{R}-\mathrm{P}}$
$=17414 \mathrm{~W}$
Secondary 1 service $I^{2} R$ loss $=12026 \mathrm{~W} \times 1.0227^{2}$
$=12578 \mathrm{~W}$
Secondary winding eddy current loss, $P^{\prime}$ EC-S $=850 \mathrm{~W} \times 2.8952$
$=2461 \mathrm{~W}$
Total secondary winding 1 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}$
$=15039 \mathrm{~W}$
Secondary 2 service $I^{2} R$ loss $=12000 \mathrm{~W} \times 1.0227^{2}$
$=12551 \mathrm{~W}$
Secondary winding eddy current loss, $P_{\text {EC-S }}^{\prime}=1267 \mathrm{~W} \times 2.8952$ $=3668 \mathrm{~W}$
Total secondary winding 2 service loss, $P^{\prime}{ }_{\mathrm{R}-\mathrm{S}}$
$=16219 \mathrm{~W}$

Service other stray loss, $P^{\prime}{ }_{\text {OSL }}=5107 \mathrm{~W} \times 1.1930$
$=6093 \mathrm{~W}$

Total service load loss for the transformer with distorted load current,
$P_{\mathrm{R}}^{\prime}=17224 \mathrm{~W}+17414 \mathrm{~W}+15039 \mathrm{~W}+16219 \mathrm{~W}+6093 \mathrm{~W}$
$=71989 \mathrm{~W}$

To obtain the total service loss, add the tested core losses to total service load loss calculated above.
Total service loss, $P^{\prime}{ }_{\text {тотаL }}=71989 \mathrm{~W}+21700 \mathrm{~W}$
= 93689 W

## Annex B

## (informative)

## Bibliography

[B6] Blume, L.F. et al., Transformer Engineering. New York: John Wiley \& Sons, 1951.
[B1] Crepaz, Sergio, "Eddy current losses in rectifier transformers," IEEE Transactions on Power Apparatus and Systems, vol. PAS-89, no. 7, Sept./Oct. 1970.
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[B4] Forrest, J. Alan C., "Harmonic load losses in HVDC converter transformers," IEEE Transactions on Power Delivery, vol. 6, no. 1, Jan. 1991, pp. 153-157.
[B3] MIT Electrical Engineering Staff, Magnetic Circuits and Transformers. New York: John Wiley \& Sons, 1949.
[B5] Ram, B. S. et al., "Effect on harmonics on converter transformer load losses," IEEE Transactions on Power Delivery, vol. 3, no. 3, July 1988, pp. 1059-1066.


[^0]:    *A new working group has been formed to revise ANSI C34.2.

[^1]:    ${ }^{1}$ This standard has been withdrawn; however, copies can be obtained from Global Engineering, 15 Inverness Way East, Englewood, CO 80112-5704, USA, tel. (303) 792-2181.

[^2]:    ${ }^{2}$ IEEE publications are available from the Institute of Electrical and Electronics Engineers, 445 Hoes Lane, P.O. Box 1331, Piscataway, NJ 08855-1331, USA.
    ${ }^{3}$ IEEE Std 995-1987 has been withdrawn; however, copies can be obtained from Global Engineering, 15 Inverness Way East, Englewood, CO 80112-5704, USA, tel. (303) 792-2181.
    ${ }^{4}$ IEEE Std C57.12.01-1989 has been withdrawn; however, copies can be obtained from Global Engineering, 15 Inverness Way East, Englewood, CO 80112-5704, USA, tel. (303) 792-2181.
    ${ }^{5}$ Information on references can be found in Clause 2.

[^3]:    ${ }^{6}$ Refers to secondary winding phases. (Quantity $q$ in the list of symbols; see Clause 4.)

[^4]:    ${ }^{7}$ IEEE Recommended Practice for Establishing Transformer Capability When Supplying Nonsinusoidal Load Currents.

